

Generalized ovals, 2.5-dimensional additive codes, and multispreads

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Abstract

We present constructions and bounds for additive codes over a finite field in terms of their geometric counterpart, i.e. projective systems. It is known that the maximum number of $(l-1)$ -spaces in $\text{PG}(2, q)$, such that no hyperplane contains three, is given by $q^l + 1$ if q is odd. Those geometric objects are called generalized ovals. We show that cardinality $q^l + 2$ is possible if we decrease the dimension a bit. We completely determine the minimum possible lengths of additive codes over $\mathbb{F}_q$ of dimension 2.5 and give improved constructions for other small parameters. As an application, we consider multispreads in $\text{PG}(4, q)$, in particular, completing the characterization of parameters of $\mathbb{F}_4$ -linear 64-ary one-weight codes.

Keywords: additive code, projective system, generalized oval, multi-spread, one-weight code, two-weight code

1 Introduction

An additive code C is a subset of $\mathcal{R}^n$ that is closed under addition, where $\mathcal{R}$ is some mathematical structure that allows addition like e.g. a ring, a field, or an additive group. Here we will always assume that $\mathcal{R}$ is a field and that the distances between the codewords, i.e. the elements of C , are measured by

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the Hamming metric. In computer science additive codes are studied as a subclass of general block codes, containing linear codes, that has better algorithmic properties. In [14] folded Reed–Solomon codes were introduced with the property that they admit much better list-decoding algorithms than the original Guruswami–Sudan algorithm [15]. Another subclass of additive codes allowing improved decoding algorithms, see e.g. [29], and also obtained by some folding (or grouping) construction is given by so-called multiplicity codes [16, 25]. There is some renewed interest in additive codes due to applications in the construction of quantum codes, see e.g. [6, 7, 11, 21]. Also, for classical codes additive codes are interesting since they can have better parameters than linear codes, see e.g. [13]. It is well known that additive codes over $\mathbb{F}_4$ can geometrically be described by multisets of lines in a projective space over $\mathbb{F}_2$, see e.g. [4]. In general, additive codes are in one-to-one correspondence to multisets of subspaces in projective spaces, see [2], which generalizes the well-known relation between linear codes and multisets of points. Here we will mainly use the geometric language.

A classical geometric result considers the maximum number of points in a projective plane over $\mathbb{F}_q$ such that every line contains at most two of them. For odd field sizes q the maximum number is given by $q + 1$ and the geometric objects are called ovals. For even q size $q + 2$ is possible, and the geometric objects are called hyperovals. Via the subfield construction we also obtain sets of subspaces, no more than two contained in a hyperplane, with those cardinalities. For odd q we can slightly improve the construction, see e.g. Proposition 1 and Proposition 3.

For linear codes, it is a classical and important problem to determine the minimum possible length n for each minimum Hamming distance d , given the field size q and the dimension k . Due to the Griesmer bound and the Solomon–Stiffler construction, this is a finite problem for each pair of parameters q and k . So far it has been completely solved for $k \leq 8$ when $q = 2$, for $k \leq 5$ when $q = 3$, for $k \leq 4$ when $q = 4$, for $k \leq 3$ when $q \leq 9$, and for all $k \leq 2$. For additive codes there is also a Griesmer type bound, see [2, Theorem 12], which can always be attained with equality if the minimum distance d is sufficiently large [19]. Here we determine the minimum lengths of 5/2-dimensional additive codes over $\mathbb{F}_9$ for all minimum distances, see Theorem 4. For 5/2-dimensional additive codes over $\mathbb{F}_{16}$ and $\mathbb{F}_{25}$ we give partial results.

For each prime power q there exists a line spread in $\text{PG}(3, q)$, i.e. a set of lines such that each point is contained in exactly one element. The notion of t -spreads has been generalized to multispreads [18]. Here we are e.g. interested in sets of $q^3 + 1$ planes and $q^2 + 1$ lines in $\text{PG}(4, q)$ such that each point is either contained in $q + 1$ planes and no line or, alternatively, in one plane and one line. For $q = 3$ we classify all such systems and for $q = 4, 5$ we give partial results. In coding theoretic terms multispreads correspond to additive one-weight codes.

The remaining part of this paper is structured as follows. In Section 2 we introduce the necessary preliminaries. Our results on oval-like structures, i.e., no more than two subspaces contained in a hyperplane are presented in Section 3. In Section 4 we use prescribed automorphisms and integer linear

programming to obtain improved constructions for additive codes with small parameters. Multispreads are treated in Section 5. For the mentioned oval-like structure we give an alternative construction in Appendix A, which is a rare example of a non-computational construction of a code with prescribed automorphism group. List of multispreads with new parameters are listed in Appendix B. Explicit representations for the 5/2-dimensional additive codes over $\mathbb{F}_{16}$ and $\mathbb{F}_{25}$ mentioned in Theorem 5 and Theorem 6 are listed in Appendix D and Appendix C, respectively.

2 Preliminaries

Let $\mathbb{F}_q$ denote the finite field with q elements, where $q = p^l$ is a prime power and the prime is called the characteristic of $\mathbb{F}_q$. An additive code C of length n over the alphabet $\mathcal{A} = \mathbb{F}_{q'}$ is a subset of $\mathbb{F}_{q'}^n$ such that $u + v \in C$ for all $u, v \in C$. It turns out that each code C that is additive over $\mathbb{F}_{q'}$ is linear over some subfield $\mathbb{F}_q \leq \mathbb{F}_{q'}$, i.e., $\alpha u + \beta v \in C$ for all $u, v \in C$ and all $\alpha, \beta \in \mathbb{F}_q$ [1, 2]. So, we use the notation $[n, r/h, d]_q^h$ for an additive code C that is linear over $\mathbb{F}_q$ and has length n , minimum distance d , alphabet $\mathcal{A} = \mathbb{F}_{q^h}$, and size q^r , where $r \in \mathbb{N}$. We also call $k = r/h \in \mathbb{Q}$ the dimension of C , so that $\#C = \#\mathcal{A}^k$ and an $[n, k, d]_q^1$ additive code is an $[n, k, d]_q$ linear code. Note that k can be fractional. An $[n, k, d]_q$ linear code C can be defined as the rowspace of a $k \times n$ matrix with entries in $\mathbb{F}_q$, called a generator matrix for C . Similarly, an $[n, r/h, d]_q^h$ additive code C can be defined as the $\mathbb{F}_q$ -space spanned by the rows of an $r \times n$ matrix G with entries in $\mathbb{F}_{q^h}$, again called a *generator matrix* for C . Let $\mathcal{B}$ be a basis for $\mathbb{F}_{q^h}$ over $\mathbb{F}_q$ and write out the elements of G over the basis $\mathcal{B}$ to obtain an $r \times nh$ matrix $\tilde{G}$ with entries from $\mathbb{F}_q$. Here we assume that the columns of $\tilde{G}$ are grouped together into n groups of h columns and say that $\tilde{G}$ is a subfield generator matrix for C .

Let $\text{PG}(v-1, q)$ denote the projective geometry over $\mathbb{F}_q^v$. While we will use the geometric language, we will use the algebraic dimension for subspaces, i.e., points are 1-dimensional, lines are 2-dimensional, planes are 3-dimensional, solids are 4-dimensional, and hyperplanes are $(v-1)$ -dimensional subspaces. In general, a t -space is a t -dimensional subspace. By $[t]_q := \frac{q^t-1}{q-1}$ we denote the number of points of a t -space. Given a generator matrix G of a linear $[n, k, d]_q$ code, the columns of G span 1-dimensional subspaces, i.e. points in $\text{PG}(k-1, q)$ (allowing the 0-dimensional space as a degenerated case or forbidding zero columns in G). This induces the well-known correspondence between linear codes and multisets of points in projective spaces, see e.g. [10]. More precisely, a minimum distance d of the code relates to the geometric property that at most $n-d$ elements are contained in a hyperplane. Similarly, the groups of h subsequent columns in a subfield generator matrix $\tilde{G}$ span subspaces of dimension at most h such that at most $n-d$ elements are contained in each hyperplane, if the additive code has length n and minimum distance d . By $\mathcal{X}_G(C)$ we define the multiset of the n subspaces spanned by the n blocks of h

columns of $\tilde{G}$ in this way. We say that C is faithful if all elements of $\mathcal{X}_G(C)$ have dimension h and unfaithful otherwise. This is indeed a property of the code C and does not depend on the choice of a generator matrix G or the choice of a basis $\mathcal{B}$, see e.g. [2], so that we also write $\mathcal{X}(C)$. We remark that a linear code C , i.e. an additive code with $h = 1$ is unfaithful iff an arbitrary generator matrix for C contains a column consisting entirely of zeroes.

Example 1. Writing $\mathbb{F}_4 \simeq \mathbb{F}_2[\omega]/(\omega^2 + \omega + 1)$, we can start with the generator matrix of a linear $[5, 2, 4]_4$ code, interpret it as the generator matrix of an additive code and use the basis $\mathcal{B}$ to obtain the example

$$\begin{pmatrix} 0 & 1 & 1 & 1 & 1 \\ 1 & 0 & 1 & \omega & \omega^2 \end{pmatrix} \rightarrow \begin{pmatrix} 0 & 1 & 1 & 1 & 1 \\ 0 & \omega & \omega & \omega & \omega \\ 1 & 0 & 1 & \omega & \omega^2 \\ \omega & 0 & \omega & \omega^2 & 1 \end{pmatrix} \rightarrow \begin{pmatrix} 00 & 10 & 10 & 10 & 10 \\ 00 & 01 & 01 & 01 & 01 \\ 10 & 00 & 10 & 01 & 11 \\ 01 & 00 & 01 & 11 & 10 \end{pmatrix}.$$

The first matrix is a generator matrix of a $[5, 2, 4]_4$ code, which geometrically is the set of all five points in $\text{PG}(1, 4)$. The second matrix is a generator matrix of a $[5, 4/2, 4]_2^2$ (additive) code, which is linear over $\mathbb{F}_4$ by construction (called subfield construction). The third matrix is the corresponding subfield generator matrix, where the five pairs of columns span lines, i.e. we geometrically have a line spread of $\text{PG}(3, 2)$.

Definition 1. A projective $h - (n, r, s)_q$ system is a multiset $\mathcal{S}$ of n subspaces of $\text{PG}(r - 1, q)$ of dimension at most h such that each hyperplane contains at most s elements of $\mathcal{S}$ and some hyperplane contains exactly s elements of $\mathcal{S}$. We say that $\mathcal{S}$ is faithful if all elements have dimension h . A projective $h - (n, r, s)_q$ system $\mathcal{S}$ is a projective $h - (n, r, s, \mu)_q$ system if each point is contained in at most μ elements from $\mathcal{S}$ and there is some point that is contained in exactly μ elements from $\mathcal{S}$.

Note that the elements of $\mathcal{S}$ span the entire ambient space $\text{PG}(r - 1, q)$ iff $s < n$. If $\mathcal{S}$ is a projective $h - (n, r, s)_q$ system that is not faithful, then we can easily construct a projective $h - (n, r, \leq s)_q$ system $\mathcal{S}'$ by replacing each element $S \in \mathcal{S}$ with dimension smaller than h by an arbitrary h -space containing S .

Definition 2. By $n_q(r, h; s)$ we denote the maximum number n such that a projective $h - (n, r, s)_q$ system exists.

From the subfield construction we conclude $n_q(rh, h; s) \geq n_{q^h}(r, 1; s)$. In general, projective $h - (n, r, s)_q$ systems (with $s < n$) are in one-to-one correspondence to additive codes:

Theorem 1. ([2, Theorem 5]) If C is an additive $[n, r/h, d]_q^h$ code with generator matrix G , then $\mathcal{X}_G(C)$ is a projective $h - (n, r, n - d)_q$ system $\mathcal{S}$, and conversely, each projective $h - (n, r, s)_q$ system $\mathcal{S}$ defines an additive $[n, r/h, n - s]_q^h$ code C .

We have that C is faithful iff $\mathcal{S}$ is faithful. Whenever the specific choice of a generator matrix G or a subfield generator matrix $\tilde{G}$ is irrelevant, we write $\mathcal{S} = \mathcal{X}(C)$ or $C = \mathcal{X}^{-1}(\mathcal{S})$. Unfaithful projective systems can arise by projection. If we e.g. start with the faithful projective $2 - (5, 4; 1)_2$ system from Example 1, then projection through an arbitrary point yields an unfaithful projective $2 - (5, 3; 1)_2$ system consisting of four lines and one point (obtained from the line containing the projection point). So clearly, we have $n_q(r, h; s) \geq n_q(r', h; s)$ for all $r \leq r'$.

Definition 3.

$$\bar{n}_q(r, h; s) := n_q(\lceil r/h \rceil, 1; s) \quad (1)$$

In words, $\bar{n}_q(r, h; s)$ is the size of the largest projective $h - (n, r, s)_q$ system that we can obtain starting from a linear code over $\mathbb{F}_{q^h}$ interpreted as a multiset of points via the subfield construction by an iterative application of projection. Whenever $\bar{n}_q(r, h; s) < n_q(r, h; s)$ we say that additive codes outperform linear codes for the corresponding parameters, which is especially interesting if r/h is integral.

We can also utilize linear codes to obtain upper bounds for $n_q(r, h; s)$.

Definition 4. For a faithful projective $h - (n, r, s)_q$ system $\mathcal{S}$ let $\mathcal{P}(\mathcal{S})$ denote the multiset of points that we obtain by replacing each element of $\mathcal{S}$ by its contained $[h]_q$ points.

Lemma 1. ([19, Lemma 4]) Let $\mathcal{S}$ be a faithful projective $h - (n, r, s, \mu)_q$ system. Then $\mathcal{P}(\mathcal{S})$ is a faithful projective $1 - (n', r, s', \mu)_q$ system, where $n' = n[h]_q$ and $s' = n \cdot [h-1]_q + s \cdot q^{h-1}$. Moreover, $C := \mathcal{X}^{-1}(\mathcal{P}(\mathcal{S}))$ is a q^{h-1} -divisible linear $[n', r, d']_q$ code C with maximum weight at most $n \cdot q^{h-1}$, where $d' = q^{h-1} \cdot (n-s)$.

Here a linear code is called Δ -divisible if the weights of all codewords are divisible by Δ .

Definition 5. The strong coding upper bound for $n_q(r, h; s)$ is the largest integer n such that a linear code with properties as specified in Lemma 1 exists. Ignoring the conditions on divisibility and the maximum weight, the maximum possible length n is called the weak coding upper bound.

Example 2. Since the existence of a $[84, 8, 40]_2$ code and the non-existence of a $[87, 8, 42]_2$ code are known, we obtain $n_2(8, 2; 8) \leq 28$, i.e. the weak coding upper bound for $n_2(8, 2; 8)$ is 28.

One specific lower bound for the length n of an $[n, k, d]_q$ code is the so-called Griesmer bound [12, 28]

$$n \geq \sum_{i=0}^{k-1} \left\lceil \frac{d}{q^i} \right\rceil =: g_q(k, d). \quad (2)$$

Interestingly enough, this bound can always be attained with equality if the minimum distance d is sufficiently large and a nice geometric construction was

given by Solomon and Stiffler [28]. For additive codes we also have a Griesmer bound via the reformulation as a projective system $\mathcal{S}$ and Lemma 1 by only using the Griesmer bound for linear codes

$$\begin{aligned} n &\geq \left\lceil \frac{g_q(r, d \cdot q^{h-1})}{[h]_q} \right\rceil = \left\lceil \frac{\sum_{i=0}^{r-1} \lceil d \cdot q^{h-1-i} \rceil}{[h]_q} \right\rceil \\ &= d + \left\lceil \frac{\sum_{i=1}^{r-h} \left\lceil \frac{d}{q^i} \right\rceil}{[h]_q} \right\rceil = d + \left\lceil \frac{g_q(r-h+1, d) - d}{[h]_q} \right\rceil, \end{aligned}$$

see e.g. [2, Theorem 12] or [19, Lemma 15]. Here we also speak of the Griesmer upper bound, which is 30 in our example since the Griesmer bound implies that no $[93, 8, 46]_2$ code exists but cannot rule out the existence of a $[90, 8, 44]_2$ code. One of the main results of [19] is that the mentioned Griesmer bound for additive codes can always be attained if the minimum distance d is sufficiently large. Thus, also the determination of $n_q(r, h; s)$ is a finite problem for each triple of parameters (q, r, h) .

3 At most two subspaces in a hyperplane – generalized ovals

An oval in $\text{PG}(2, q)$ is a set $\mathcal{O}$ of $q+1$ points such that no three points are on a line. If the field size q is odd, then each oval is a conic and each set of $q+2$ points does contain a line incident with at least three points [27]. This is different if q is even, where other constructions exist and cardinality $q+2$ can indeed be reached, where the geometric object then is called hyperoval. Given an arbitrary set of points $\mathcal{S}$ in $\text{PG}(2, q)$, a line that contains two points from $\mathcal{S}$ is called a secant and a line that contains exactly one point from $\mathcal{S}$ is called a tangent. Given an oval $\mathcal{O}$ in $\text{PG}(2, q)$, where q is odd, each point in $\mathcal{O}$ is contained in q secants and a unique tangent. Applying the subfield construction to a hyperoval in $\text{PG}(2, q^2)$, where q is even, gives a faithful projective $2 - (q^2 + 2, 6, 2, 1)_q$ system $\mathcal{S}$. Projection through a point P then gives a projective $2 - (q^2 + 2, 5, 2)_q$ system that is faithful iff P is not contained in one of the elements from $\mathcal{S}$. Arcs, ovals, and hyperovals were generalized by replacing their points with l -spaces and their maximum possible cardinality in $\text{PG}(3l-1, q)$ can indeed be obtained by applying the subfield construction in $\text{PG}(2, q^l)$ [30]. For the relation to (translation) generalised quadrangles we refer to [31, 32].

Starting from an oval in $\text{PG}(2, q^2)$, applying the subfield construction and projection through a point, yields a projective $2 - (q^2 + 1, 5, 2)_q$ system. The following result shows that we can improve upon that.

Proposition 1.

$$n_q(5, 2; 2) \geq q^2 + 2$$

Proof. W.l.o.g. we assume that q is odd, consider an oval $\mathcal{O}$ in $\text{PG}(2, q^2)$, and fix some element $P \in \mathcal{O}$. Removing P from $\mathcal{O}$ and applying the subfield construction gives a faithful projective $2 - (q^2, 6, 2, 1)_q$ system $\mathcal{S}$. Denote the line in $\text{PG}(5, q)$ that corresponds to P in $\text{PG}(2, q^2)$ by L . Denote the unique tangent line of P in $\mathcal{O}$ by T and let S be the corresponding 4-space in $\text{PG}(5, q)$. By construction S is disjoint to the lines in $\mathcal{S}$. Applying projection through an arbitrary point in L gives a faithful projective $2 - (q^2, 5, 2, 1)_q$ system $\mathcal{S}'$ whose elements are disjoint to a plane π . Denoting the image of L by Q we construct $\mathcal{S}''$ by adding two different lines incident with Q and π to $\mathcal{S}'$. To conclude that $\mathcal{S}''$ is a faithful projective $2 - (q^2 + 2, 5, 2, 2)_q$ system, it remains to check that every hyperplane contains at most 2 elements of $\mathcal{S}''$. So, if H is a hyperplane that contains π , then H cannot contain elements from $\mathcal{S}'$ and only contains the two additional lines in π . If H is a hyperplane that intersects π in a line, then it contains at most one of the two lines in π and it remains to show that it cannot contain two elements from $\mathcal{S}'$. To this end, we observe that any pair of lines in $\mathcal{S}'$ spans a solid that is disjoint to Q . $\square$

We remark that it is known that for odd q an arc of size q in $\text{PG}(2, q)$ can always be extended to an oval i.e. a conic [26, 27].

In order to obtain an upper bound for $m_q(5, 2; 2)$ we can mimic the argument for the maximum cardinality of arcs in $\text{PG}(2, q)$.

Lemma 2. *We have $n_q(5, 2; s) \leq (s - 1)(q^2 + q + 1) + 1$ for each $s \geq 2$. If a projective system misses this number by less than q , then it has to be faithful and no two lines intersect in a point.*

Proof. Let $\mathcal{S}$ be a projective $2 - (n, 5, s)_q$ system. Assume that $L \in \mathcal{S}$ is an arbitrary 2-dimensional element. Projection through L yields a projective $2 - (n - c, 3, s - c)_q$ system $\mathcal{S}'$, where c denotes the multiplicity of L in $\mathcal{S}$. Since $n_q(3, 2; s') = s' \cdot (q^2 + q + 1)$ we conclude the statement. If no element of $\mathcal{S}'$ has dimension 2 then we assume that L is spanned by two different arbitrary 1-dimensional elements in $\mathcal{S}$. Projection through L yields a projective $2 - (n - c, 3, s - c)_q$ system $\mathcal{S}''$, where c denotes the sum of the multiplicities of the points in L w.r.t. $\mathcal{S}$. Here we can proceed as before. Otherwise, we clearly have $\#\mathcal{S} \leq s$.

For the second part we remark that each projective $2 - (n', 3, s')_q$ system satisfies $n' \leq (q^2 + q + 1)s' - (q - 1)$ if it is unfaithful or contains two lines that intersect in a point. $\square$

So we e.g. have $n_q(5, 2; 2) \leq q^2 + q + 2$ and each projective $2 - (n, 5, 2, \mu)_q$ system with $n > q^2 + 2$ satisfies $\mu = 1$ and is faithful.

Lemma 3. *If $\mathcal{S}$ is a projective l -($n, 2l + j, 2, \mu$) $_q$ system, $l \geq 2$, $j \geq 1$, that contains an $(l - i)$ -space or two i -intersecting spaces, $i \in \{0, \dots, l\}$, then*

$$n \leq ([l + j]_q - [i + j]_q)/[j]_q + 2 = \frac{q^j(q^l - q^i)}{q^j - 1} + 2. \quad (3)$$

In particular,

- (i) $n_q(2l + j, l; 2) \leq [l + j]_q/[j]_q + 1$;
- (ii) *if $n > ([l + j]_q - [j + 1]_q)/[j]_q + 2$, then the system is faithful and $\mu = 1$.*

Proof. If the system contains an $(l - i)$ -space or two i -intersecting spaces, then there is a $(2l - i)$ -space L' containing as subspaces two elements s, s' of $\mathcal{S}$. Considering an l -space L such that $s \subseteq L \subset L'$, we get that any element of $\mathcal{S} \setminus \{s\}$ lies in at least $[j]_q$ hyperplanes containing L . There are $[l + j]_q$ such hyperplanes, but $[i + j]_q$ of them are superspaces of S' and hence contain both s and s' . It follows that $|\mathcal{S} \setminus \{s, s'\}| \leq [l + j]_q - [i + j]_q$, which proves (3).

(i) and (ii) are special cases of (3) corresponding to $i = 0$ and $i = 1$, respectively. $\square$

Corollary 1. $n_q(2l + 1, l; 2) \leq \sum_{i=1}^l q^i + 2$. *Moreover, if an l -($n, 2l + 1, 2; \mu$) $_q$*

system is unfaithful or $\mu > 1$, then $n \leq \sum_{i=2}^l q^i + 2$.

More generally, we have the following.

Proposition 2. *If $\mathcal{S}$ is a projective l -($n, sl + j, s, \mu$) $_q$ system, $l, s \geq 2$, $j \geq 0$, such that the span of some s of its elements has dimension at most $sl - i$, then (3) holds. In particular,*

$$n_q(sl + j, l; s) \leq [l + j]_q + s - 1.$$

Proof sketch. The proof is similar to that of Lemma 3. L' is a $(sl - i)$ -space including s elements of $\mathcal{S}$; L is a $(s - 1)l$ -subspace of L' including $s - 1$ elements of $\mathcal{S}$. $\square$

We remark that the proof of Lemma 2 also shows that a hypothetical faithful projective $2 - (q^2 + q + 2, 5, 2)_q$ system $\mathcal{S}$ has the property that the number of lines per hyperplane is always even, i.e. all $q^2 + q + 1$ lines through an element of $\mathcal{S}$ contain a second (disjoint) line. Considering the $q^2 + q + 1$ hyperplanes through a line that is not contained in $\mathcal{S}$ gives the condition that $q^2 + q + 2 = q(q + 1) + 2$ is even, which is always satisfied – different as in the situation for arcs in $\text{PG}(2, q)$. Note that the upper bound from Lemma 2 can be attained for $q = 2$. To this end, we remark that a vector space partition of type $3^1 2^{q^3}$ of $\text{PG}(4, q)$, i.e. a faithful projective $2 - (q^3, 5, s, 1)_q$ system whose elements all are disjoint to some plane π , has the property that each hyperplane contains either no or q lines (depending on whether π is contained in the hyperplane or not), i.e. we have $s = q$. Such a partition can e.g. be constructed from lifted MRD codes.

Theorem 2. *If s contains a factor that is coprime to q , then we have $n_q(5, 2; s) < (s - 1) \cdot (q^2 + q + 1) + 1$.*

Proof. Assume that $\mathcal{S}$ is a faithful projective $2 - ((s - 1)(q^2 + q + 1) + 1, 5, 2, \mu')_q$ system. Due to Lemma 2 we have $\mu' = 1$. Replacing each element of $\mathcal{S}$ by its contained $q + 1$ points we obtain a faithful projective $1 - ((q + 1) \cdot \#\mathcal{S}, 5, s, 1)_q$ system $\mathcal{S}$, i.e. a set $\mathcal{M}$ of $(q + 1) \cdot ((s - 1)(q^2 + q + 1) + 1)$ points in $\text{PG}(4, q)$ such that every hyperplane contains at most s elements from $\mathcal{M}$. Since each hyperplane H contains either s or no elements from $\mathcal{S}$, we see that H intersects $\mathcal{M}$ in $(s - 1) \cdot (q^2 + q + 1) + 1 + sq$ or $(s - 1) \cdot (q^2 + q + 1) + 1$ points. In other words, the linear code corresponding to $\mathcal{M}$ is a projective $[(q + 1) \cdot ((s - 1)(q^2 + q + 1) + 1), 5, \{w_1, w_2\}]_q$ code, where $w_1 = w_2 + sq$ and $w_2 = q \cdot ((s - 1)(q^2 + q + 1) + 1)$, i.e. a projective two-weight code. However, the difference of the occurring non-zero weights equals sq . Since it has to be a power of the characteristic of $\mathbb{F}_q$, see [8, Corollary 2], we obtain a contradiction if s contains a factor that is coprime to q . $\square$

So we e.g. have $n_q(5, 2; 2) < q^2 + q + 2$ for odd q . For $s = 2$ the strongly regular graph corresponding to the utilized linear code has parameters (q^5, k, λ, μ) , where $k = (q^2 - 1) \cdot (q^2 + q + 2)$, $\lambda = q^3 + 2q^2 + q - 2$, and $\mu = q^3 + 2q^2 + 3q + 2$. Interestingly enough, the case for $q = 3$ is marked as *open* at <https://aeb.win.tue.nl/graphs/srg/srgtab201-250.html>. For $q = 4$ a strongly regular graph with parameters $(1024, 330, 98, 110)$ indeed exists [24], even as linear codes, i.e. as a projective $[110, 5, \{80, 88\}]_4$ code [9] and as a projective $[330, 10, \{160, 176\}]_2$ code [22, 23]. We have computationally checked that none of the ten $[110, 5, \{80, 88\}]_4$ codes listed in [9, Appendix B] can be partitioned into 22 lines, when considered as a set of points in $\text{PG}(4, 4)$. An example showing $n_4(5, 2; 2) \geq 20 = q^2 + q$ is given by $\begin{pmatrix} 101\omega^2\omega \\ 01\omega^2\omega_1 \end{pmatrix}, \begin{pmatrix} 10\omega\omega^21 \\ 01\omega^21\omega \end{pmatrix}, \begin{pmatrix} 100\omega^21 \\ 01000 \end{pmatrix}, \begin{pmatrix} 10000 \\ 01\omega^201 \end{pmatrix}, \begin{pmatrix} 10\omega^2\omega^2\omega \\ 01\omega^2\omega^2\omega \end{pmatrix}, \begin{pmatrix} 10001 \\ 01100 \end{pmatrix}, \begin{pmatrix} 10\omega1\omega \\ 011\omega^2\omega \end{pmatrix}, \begin{pmatrix} 10\omega^210 \\ 011\omega1 \end{pmatrix}, \begin{pmatrix} 10111 \\ 0111\omega \end{pmatrix}, \begin{pmatrix} 1001\omega \\ 01001 \end{pmatrix}, \begin{pmatrix} 1\omega^201\omega^2 \\ 0011\omega \end{pmatrix}, \begin{pmatrix} 1\omega10\omega^2 \\ 00011 \end{pmatrix}, \begin{pmatrix} 110\omega^2\omega \\ 001\omega^21 \end{pmatrix}, \begin{pmatrix} 100\omega\omega \\ 001\omega\omega \end{pmatrix}, \begin{pmatrix} 01010 \\ 00101 \end{pmatrix}, \begin{pmatrix} 1\omega^20\omega^2\omega \\ 00110 \end{pmatrix}, \begin{pmatrix} 1\omega\omega^20\omega^2 \\ 00010 \end{pmatrix}, \begin{pmatrix} 010\omega^2\omega^2 \\ 00100 \end{pmatrix}, \begin{pmatrix} 1001\omega^2 \\ 001\omega0 \end{pmatrix}, \begin{pmatrix} 110\omega\omega \\ 001\omega^20 \end{pmatrix}$, where we identify $\mathbb{F}_4 \cong \mathbb{F}_2[\omega]/(\omega^2 + \omega + 1)$. We have computationally checked that a hypothetical $2 - (21, 5; 2)_4$ or a $2 - (22, 5; 2)_4$ system cannot have a non-trivial automorphism group.

The case of field size $q = 3$ can be solved exactly, i.e. we have $n_3(5, 2; 2) = 12 = q^2 + q$. The inequivalent faithful projective $2 - (n, 5, 2)_3$ systems can be easily enumerated. There are exactly six faithful projective $2 - (12, 5, 2)_3$ systems and no faithful projective $2 - (13, 5, 2)_3$ system. More precisely, we have verified the numbers stated in [2, Table 3, line $r = 5$] and [2, Remark 27]. The number of unfaithful projective $2 - (n, 5, 2)_3$ systems is given by 1, 5, 21, 26, 9, 1, 1 for $n = 4, \dots, 10$ and there is no unfaithful $2 - (11, 5, 2)_3$ system. In principle, the multiset of points covered by a faithful projective system can admit several partitions. Interestingly enough, for our parameters all partitions are equivalent except for two cases for $n = 10$, where trading switches eight lines. For more details on trades we refer e.g. to [17].

The construction in Proposition 1 can also be generalized to ovals in $\text{PG}(2, q^l)$ for $l \geq 2$.

Proposition 3. *For $l \geq 2$ we have $n_q(\lfloor 2.5l \rfloor, l; 2) \geq q^l + 2$.*

Proof. W.l.o.g. we assume that q is odd and consider an oval $\mathcal{O}$ in $\text{PG}(2, q^l)$ and fix some element $P \in \mathcal{O}$. Removing P from $\mathcal{O}$ and applying the subfield construction gives a faithful projective $l - (q^l, 3l, 2, 1)_q$ system $\mathcal{S}$. Denote the l -space in $\text{PG}(3l - 1, q)$ that corresponds to P in $\text{PG}(2, q^l)$ by L . Denote the unique tangent line of P in $\mathcal{O}$ by T and let S be the corresponding $2l$ -space in $\text{PG}(3l - 1, q)$. By construction S is disjoint to the l -spaces in $\mathcal{S}$. Applying projection through an arbitrary $\lfloor l/2 \rfloor$ -space in L gives a faithful projective $l - (q^l, \lfloor 2.5l \rfloor, 2, 1)_q$ system $\mathcal{S}'$ whose elements are disjoint to an $(l + 1)$ -space π . Denoting the image of L by Q we construct $\mathcal{S}''$ by adding (to $\mathcal{S}'$) two different l -spaces including Q and spanning π (here we use that $2l \geq \dim(\pi) + \dim(Q)$, which comes from the number $\lfloor l/2 \rfloor$ of collapsed dimensions). To conclude that $\mathcal{S}''$ is a faithful projective $l - (q^l + 2, \lfloor 2.5l \rfloor, 2, 2)_q$ system, it remains to check that every hyperplane contains at most 2 elements of $\mathcal{S}''$. So, if H is a hyperplane that includes π , then H cannot contain elements from $\mathcal{S}'$ and only contains the two additional l -spaces in π . If H is a hyperplane that does not include the whole π , then it contains at most one of the two l -spaces in π and it remains to show that it cannot contain two elements from $\mathcal{S}'$ and one l -space in π . To this end, we observe that any pair of l -spaces in $\mathcal{S}'$ spans a $2l$ -space that is disjoint to Q ; hence, such two l -spaces and one of the two subspaces that include Q span the entire space and cannot lie in a hyperplane. $\square$

Theorem 3. *For odd q and $l \geq 2$ we have $n_q(2l + 1, l; 2) < \lfloor l + 1 \rfloor_q + 1$.*

Proof. Assume that $\mathcal{S}$ is a faithful projective $l - (\lfloor l + 1 \rfloor_q + 1, 2l + 1, 2, \mu')_q$ system. Due to Lemma 3 we have $\mu' = 1$. Replacing each element of $\mathcal{S}$ by its contained $\lfloor l \rfloor_q$ points we obtain a faithful projective $1 - (\lfloor l \rfloor_q \cdot \#\mathcal{S}, 2l + 1, s, 1)_q$ system $\mathcal{S}$, i.e. a set $\mathcal{M}$ of $\lfloor l \rfloor_q \cdot (\lfloor l + 1 \rfloor_q + 1)$ points in $\text{PG}(2l, q)$ such that every hyperplane contains at most s elements from $\mathcal{M}$. Since each hyperplane H contains either two or no elements from $\mathcal{S}$, we see that H intersects $\mathcal{M}$ in $(\lfloor l + 1 \rfloor_q + 1) \cdot \lfloor l - 1 \rfloor_q + 2q^{l-1}$ or $(\lfloor l + 1 \rfloor_q + 1) \cdot \lfloor l - 1 \rfloor_q$ points. In other words, the linear code corresponding to $\mathcal{M}$ is a projective two-weight code with weight difference $2q^{l-1}$. Since it has to be a power of the characteristic of $\mathbb{F}_q$, see [8, Corollary 2], we obtain a contradiction for odd q . $\square$

We remark that the statement also holds for $l = 1$, since for odd q there are no hyperovals.

Underlying our geometric constructions seems the following recipe: Start with a linear code of a large field and consider it as a multiset of points. After removing a point (or possibly several) we apply the subfield construction and project through some subspaces contained in the image of a removed point. Afterwards it is sometimes possible to add more subspaces than removed before. Of course this approach is not always successful. Starting from an ovoid over $\mathbb{F}_4$

we obtain $n_2(8, 2; 5) \geq 17$, which is tight. However, we also have $n_2(7, 2; 5) = 17$, see e.g. [19, Theorem 14], i.e. no improvement possible for these parameters. In the proof of the following construction the “removed” point is denoted as S_1 . If we add it as the last column to a generator matrix of the corresponding linear code we get the generator matrix of the doubly-extended Reed–Solomon code – an s -arc of size $q^l + 1$ in geometrical terms, where s and l are parameters of our construction. The subspace S_2 is the analog of the tangent line through S_1 . But now we need that the following generalization of the “tangent” property: any $s - 1$ points of the arc are disjoint with S_2 . For our situation we will present an algebraic proof.

Proposition 4. *For $l, s \geq 2$ we have $n_q(ls + \lfloor 0.5l \rfloor, l; s) \geq q^l + 2$.*

Proof. We start with the extended Reed–Solomon code $R(s)$ with the generator matrix

$$G_s = \begin{pmatrix} 1 & 1 & 1 & \dots & 1 \\ 0 & \alpha^1 & \alpha^2 & \dots & \alpha^{q^l-1} \\ 0 & \alpha^2 & \alpha^4 & \dots & \alpha^{2(q^l-1)} \\ \vdots & \vdots & \vdots & \ddots & \vdots \\ 0 & \alpha^{s-1} & \alpha^{2s-2} & \dots & \alpha^{(s-1)(q^l-1)} \\ 0 & \alpha^s & \alpha^{2s} & \dots & \alpha^{s(q^l-1)} \end{pmatrix},$$

where α is a primitive element of $\mathbb{F}_{q^l}$. It is a linear $[q^l, s + 1, q^l - s]_{q^l}$ code. We consider the $(s + 1)$ -dimensional column space V_{s+1} of the matrix above; the columns are treated as points (1-dimensional subspaces) $a_0, \dots, a_{q^l-1}$ in this space.

We denote by S_i the i -dimensional subspace of the column space consisting of all columns with first $s + 1 - i$ zeros. We claim the following:

- (*) *The span of any $s + 1 - i$ columns of G_s is an $(s + 1 - i)$ -dimensional space disjoint with S_i , $i = 1, \dots, s$. The claim follows from the non-zero determinant of the Vandermonde matrix formed by the upper $s + 1 - i$ positions of the chosen $s + 1 - i$ columns.*

Now, we consider the $\mathbb{F}_{q^l}$ -space V_{s+1} as an $(sl + l)$ -dimensional $\mathbb{F}_q$ -space, points $a_0, \dots, a_{q^l-1}$ as l -subspaces. Let π be projecting of V_{s+1} onto an $(sl + \lfloor l/2 \rfloor)$ -dimensional $\mathbb{F}_q$ -space such that $\dim_{\mathbb{F}_q} \pi(S_1) = \dim_{\mathbb{F}_q} S_1 - \lfloor l/2 \rfloor = \lfloor l/2 \rfloor$. We choose two arbitrary l -subspaces b, b' of $\pi(V_{s+1})$ such that $\pi(S_1) \subseteq b \cap b'$ and $b + b' = \pi(S_2)$ (we can do this because $\dim b + \dim b' = l + l \geq \lfloor l/2 \rfloor + \lfloor l/2 \rfloor + l = \dim \pi(S_1) + \dim \pi(S_2)$).

To complete the proof, we have to show that the l -subspaces $\pi(a_0), \dots, \pi(a_{q^l-1}), b, b'$ form a projective l -($q^l + 2, ls + l - 1, s$) $_q$ system; that is, any $s + 1$ of them span the space $\pi(V_{s+1})$.

a) Any $s + 1$ of $a_0, \dots, a_{q^l-1}$ span V_{s+1} ; therefore, any $s + 1$ of $\pi(a_0), \dots, \pi(a_{q^l-1})$ span $\pi(V_{s+1})$.

- b) From (*), $i = 1$, any s of $\pi(a_0), \dots, \pi(a_{q^l-1})$ span an sl -space disjoint with $\pi(S_1)$. Since $\pi(S_1) \subset b$, we have that b (similarly, b') and any s of $\pi(a_0), \dots, \pi(a_{q^l-1})$ span an $sl + \lfloor l/2 \rfloor$ -space, i.e., $\pi(V_{s+1})$.
- c) Finally, from (*), $i = 2$, any $s - 1$ of $\pi(a_0), \dots, \pi(a_{q^l-1})$ span an $(s - 1)l$ -space disjoint with $\pi(S_2)$. Since $\pi(S_2) = b + b'$, we have that b, b' , and any $s - 1$ of $\pi(a_0), \dots, \pi(a_{q^l-1})$ span an $(s - 1)l + l + \lfloor l/2 \rfloor$ -space, i.e., again $\pi(V_{s+1})$. $\square$

4 Prescribing automorphisms and integer linear programming

The determination of $n_q(r, h; s)$ is a hard problem in general, since it is already for the special case $h = 1$, i.e. for linear codes. So, it makes sense to consider small parameters. For $h = 2$ and $r \leq 2$ we technically have $n_q(r, 2; s) = \infty$ since we can take as many copies of the ambient space as elements, which are not contained in any hyperplane. In $PG(2, q)$ hyperplanes and lines coincide, so that $n_q(3, 2; s) = [3]_q \cdot s$, i.e. we can take each of the $[3]_q$ lines s times. Also the situation in $PG(3, q)$ still allows a complete analytical solution, i.e. we have $n_q(4, 2; s) = \frac{[4]_q}{[2]_q} \cdot s = (q^2 + 1) \cdot s$, see [19, Theorem 8]. The determination of $n_2(5, 2; s)$, $n_2(6, 2; s)$ was completed in [3] and the determination of $n_2(7, 2; s)$ was completed in [20]. Here we complete the determination of $n_3(5, 2; s)$.

Projective systems can be easily formulated as feasible solutions of integer linear programs. As variables we use $x_S \in \mathbb{N}$ for each h -space in $PG(r - 1, q)$ (assuming a faithful projective system). The conditions are given by $\sum_{S \leq H} x_S \leq s$ for each hyperplane H . Since those ILPs are rather large even for small parameters q, r , and h , a common technique to reduce the problem size is to assume a subgroup of the automorphism group. Via this approach we can only obtain lower bounds for $n_q(r, h; s)$. In our subsequent lists of generator matrices for the subspaces of a projective system exponents mark orbit representatives and the value in the exponent is the orbit size.

Theorem 4. *We have*

- $n_3(5, 2; 13t) = 121t$ for $t \geq 1$;
- $n_3(5, 2; 13t - 1) = 121t - 10$ for $t \geq 1$;
- $n_3(5, 2; 13t - 2) = 121t - 20$ for $t \geq 1$;
- $n_3(5, 2; 13t - 3) = 121t - 30$ for $t \geq 1$;
- $n_3(5, 2; 13t - 4) = 121t - 40$ for $t \geq 1$;
- $n_3(5, 2; 13t - 5) = 121t - 50$ for $t \geq 1$;
- $n_3(5, 2; 13t - 6) = 121t - 60$ for $t \geq 1$;
- $n_3(5, 2; 13t - 7) = 121t - 67$ for $t \geq 1$;

- $n_3(5, 2; 13t - 8) = 121t - 77$ for $t \geq 1$;
- $n_3(5, 2; 13t - 9) = 121t - 87$ for $t \geq 1$;
- $n_3(5, 2; 13t - 10) = 121t - 94$ for $t \geq 1$;
- $n_3(5, 2; 13t - 11) = 121t - 104$ for $t \geq 2$ and $n_3(5, 2; 2) = 12$;
- $n_3(5, 2; 13t - 12) = 121t - 114$ for $t \geq 2$ and $n_3(5, 2; 1) = 1$.

Proof. Due to [19, Theorem 19] it remains to show the lower bounds $n_3(5, 2; 4) \geq 34$ and $n_3(5, 2; 5) \geq 44$. To this end, we have prescribed the cyclic group of order three generated by

$$\begin{pmatrix} 1 & 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 & 0 \\ 0 & 0 & 1 & 1 & 0 \\ 0 & 0 & 0 & 1 & 1 \\ 0 & 0 & 0 & 0 & 1 \end{pmatrix}$$

as an automorphism for the desired faithful $2 - (n, 5, s)_3$ systems and utilized an integer linear programming formulation. Explicit lists of lines are given as follows.

$$n_3(5, 2; 4) \geq 34: \begin{pmatrix} 00010 \\ 00001 \end{pmatrix}^1, \begin{pmatrix} 10002 \\ 00110 \end{pmatrix}^3, \begin{pmatrix} 11002 \\ 00121 \end{pmatrix}, \begin{pmatrix} 12002 \\ 00100 \end{pmatrix}, \begin{pmatrix} 10011 \\ 00120 \end{pmatrix}^3, \begin{pmatrix} 11012 \\ 00102 \end{pmatrix}, \begin{pmatrix} 12010 \\ 00112 \end{pmatrix}, \begin{pmatrix} 10021 \\ 00122 \end{pmatrix}^3, \begin{pmatrix} 11020 \\ 00101 \end{pmatrix}, \begin{pmatrix} 12022 \\ 00111 \end{pmatrix}, \begin{pmatrix} 10000 \\ 01021 \end{pmatrix}^3, \begin{pmatrix} 10010 \\ 01020 \end{pmatrix}, \begin{pmatrix} 10022 \\ 01022 \end{pmatrix}, \begin{pmatrix} 10010 \\ 01101 \end{pmatrix}^3, \begin{pmatrix} 10101 \\ 01122 \end{pmatrix}, \begin{pmatrix} 10200 \\ 01111 \end{pmatrix}, \begin{pmatrix} 10020 \\ 01100 \end{pmatrix}^3, \begin{pmatrix} 10112 \\ 01121 \end{pmatrix}, \begin{pmatrix} 10212 \\ 01110 \end{pmatrix}, \begin{pmatrix} 10020 \\ 01102 \end{pmatrix}^3, \begin{pmatrix} 10111 \\ 01120 \end{pmatrix}, \begin{pmatrix} 10210 \\ 01112 \end{pmatrix}, \begin{pmatrix} 10012 \\ 01200 \end{pmatrix}^3, \begin{pmatrix} 10120 \\ 01220 \end{pmatrix}, \begin{pmatrix} 10220 \\ 01212 \end{pmatrix}, \begin{pmatrix} 10012 \\ 01222 \end{pmatrix}^3, \begin{pmatrix} 10102 \\ 01210 \end{pmatrix}, \begin{pmatrix} 10021 \\ 01200 \end{pmatrix}^3, \begin{pmatrix} 10100 \\ 01220 \end{pmatrix}, \begin{pmatrix} 10201 \\ 01212 \end{pmatrix}, \begin{pmatrix} 10121 \\ 01010 \end{pmatrix}^3, \begin{pmatrix} 10122 \\ 01011 \end{pmatrix}, \begin{pmatrix} 10102 \\ 01012 \end{pmatrix}.$$

$$n_3(5, 2; 5) \geq 44: \begin{pmatrix} 00100 \\ 00010 \end{pmatrix}^3, \begin{pmatrix} 00100 \\ 00012 \end{pmatrix}, \begin{pmatrix} 00102 \\ 00011 \end{pmatrix}, \begin{pmatrix} 01010 \\ 00001 \end{pmatrix}^1, \begin{pmatrix} 01020 \\ 00001 \end{pmatrix}^1, \begin{pmatrix} 10010 \\ 00101 \end{pmatrix}^3, \begin{pmatrix} 11011 \\ 00111 \end{pmatrix}, \begin{pmatrix} 12012 \\ 00122 \end{pmatrix}, \begin{pmatrix} 10020 \\ 00101 \end{pmatrix}^3, \begin{pmatrix} 11022 \\ 00111 \end{pmatrix}, \begin{pmatrix} 12021 \\ 00122 \end{pmatrix}, \begin{pmatrix} 10000 \\ 01000 \end{pmatrix}^1, \begin{pmatrix} 10012 \\ 01001 \end{pmatrix}^1, \begin{pmatrix} 10021 \\ 01002 \end{pmatrix}^1, \begin{pmatrix} 10001 \\ 01110 \end{pmatrix}^3, \begin{pmatrix} 10101 \\ 01100 \end{pmatrix}, \begin{pmatrix} 10210 \\ 01121 \end{pmatrix}, \begin{pmatrix} 10002 \\ 01120 \end{pmatrix}^3, \begin{pmatrix} 10111 \\ 01112 \end{pmatrix}, \begin{pmatrix} 10200 \\ 01102 \end{pmatrix}, \begin{pmatrix} 10011 \\ 01101 \end{pmatrix}^3, \begin{pmatrix} 10102 \\ 01122 \end{pmatrix}, \begin{pmatrix} 10201 \\ 01111 \end{pmatrix}, \begin{pmatrix} 10020 \\ 01101 \end{pmatrix}^3, \begin{pmatrix} 10110 \\ 01122 \end{pmatrix}, \begin{pmatrix} 10211 \\ 01102 \end{pmatrix}, \begin{pmatrix} 10021 \\ 01120 \end{pmatrix}^3, \begin{pmatrix} 10112 \\ 01112 \end{pmatrix}, \begin{pmatrix} 10211 \\ 01210 \end{pmatrix}, \begin{pmatrix} 10100 \\ 01201 \end{pmatrix}, \begin{pmatrix} 10222 \\ 01221 \end{pmatrix}, \begin{pmatrix} 10002 \\ 01220 \end{pmatrix}^3, \begin{pmatrix} 10120 \\ 01212 \end{pmatrix}, \begin{pmatrix} 10202 \\ 01202 \end{pmatrix}, \begin{pmatrix} 10010 \\ 01202 \end{pmatrix}^3, \begin{pmatrix} 10122 \\ 01222 \end{pmatrix}, \begin{pmatrix} 10220 \\ 01211 \end{pmatrix}, \begin{pmatrix} 10012 \\ 01201 \end{pmatrix}^3, \begin{pmatrix} 10122 \\ 01221 \end{pmatrix}, \begin{pmatrix} 10221 \\ 01210 \end{pmatrix}, \begin{pmatrix} 10022 \\ 01202 \end{pmatrix}^3, \begin{pmatrix} 10102 \\ 01201 \end{pmatrix}, \begin{pmatrix} 10201 \\ 01211 \end{pmatrix}. \quad \square$$

Our next aim is to obtain bounds for $n_4(5, 2; s)$ and $n_5(5, 2; s)$. As mentioned before, the determination of $n_q(r, h; s)$ as a function of s is a finite problem since the Griesmer bound is always attained if s is sufficiently large, see [19]. In order to indicate the underlying constructions we have to introduce some notation. For each subspace S in $\text{PG}(r-1, q)$ we denote its characteristic function by χ_S , i.e. we have $\chi_S(P) = 1$ if $P \leq S$ and $\chi_S(P) = 0$ otherwise.

Definition 6. We say that a multiset of points $\mathcal{M}$ in $\text{PG}(r-1, q)$ is h -partitionable if there exist h -spaces $S_1, \dots, S_l$, for some integer l , such that $\mathcal{M} = \sum_{i=1}^l \chi_{S_i}$, i.e. $\mathcal{M}$ can be partitioned into h -spaces.

In order to describe Solomon–Stiffler type constructions we choose a chain of subspaces $S_1 \leq S_2 \leq \dots \leq S_r$ in $\text{PG}(r-1, q)$, where S_i has dimension i .

Definition 7. We say that $\sum_{i=1}^r a_i[i]$ is h -partitionable over $\mathbb{F}_q$ if the multiset of points $\sum_{i=1}^r a_i \chi_{S_i}$ in $\text{PG}(r-1, q)$ is h -partitionable, where $a_i \in \mathbb{Z}$ for all $1 \leq i \leq r$.

So, we trivially have that $[2]$ is 2-partitionable over $\mathbb{F}_q$ and the existence of line spreads in $\text{PG}(3, q)$ implies that $[4]$ is 2-partitionable over $\mathbb{F}_q$. Due to the number of points $[5]$ is not 2-partitionable over $\mathbb{F}_q$ while $(q+1) \cdot [5]$ is. For the details of this and the other constructions mentioned in the two subsequent theorems we refer the reader to [19].

Theorem 5. For $n_4(5, 2; s)$ we have the bounds and exact values stated in Table 1.

s	$n_4(5, 2; s)$	s	$n_4(\dots)$	s	$n_4(5, 2; s)$	construction
1	—	22	354	$21t - 20 \geq 22$	$341t - 328$	$t \geq 4 : (5t-4) \cdot [5] - 3[4] - [3]$
2	$20^{\text{ilp}} - 22^{\text{L.2}}$	23	371	$21t - 19 \geq 23$	$341t - 311$	$t \geq 3 : (5t-4) \cdot [5] - 2[4] - [3]$
3	$39^{\text{ilp}} - 42^{\text{T.2}}$	24	388	$21t - 18 \geq 24$	$341t - 294$	$t \geq 2 : (5t-4) \cdot [5] - [4] - [3]$
4	64	25	405	$21t - 17 \geq 25$	$341t - 277$	$t \geq 1 : (5t-4) \cdot [5] - [3]$
5	$75^{\text{ilp}} - 77$	26	418	$21t - 16 \geq 26$	$341t - 264$	$t \geq 4 : (5t-3) \cdot [5] - 3[4] - 2[3]$
6	$90^{\text{ilp}} - 94$	27	435	$21t - 15 \geq 27$	$341t - 247$	$t \geq 3 : (5t-3) \cdot [5] - 2[4] - 2[3]$
7	$107^{\text{ilp}} - 111$	28	452	$21t - 14 \geq 28$	$341t - 230$	$t \geq 2 : (5t-3) \cdot [5] - [4] - 2[3]$
8	128	29	469	$21t - 13 \geq 29$	$341t - 213$	$t \geq 1 : (5t-3) \cdot [5] - 2[3]$
9	141^{ilp}	30	482	$21t - 12 \geq 30$	$341t - 200$	$t \geq 4 : (5t-2) \cdot [5] - 3[4] - 3[3]$
10	$156^{\text{ilp}} - 158$	31	499	$21t - 11 \geq 31$	$341t - 183$	$t \geq 3 : (5t-2) \cdot [5] - 2[4] - 3[3]$
11	175^{ilp}	32	516	$21t - 10 \geq 32$	$341t - 166$	$t \geq 2 : (5t-2) \cdot [5] - [4] - 3[3]$
12	192	33	533	$21t - 9 \geq 33$	$341t - 149$	$t \geq 1 : (5t-2) \cdot [5] - 3[3]$
13	205	34	546	$21t - 8 \geq 34$	$341t - 136$	$t \geq 4 : 5t \cdot [5] - 3[4] - 4[3]$
14	222^{ilp}	35	563	$21t - 7 \geq 35$	$341t - 119$	$t \geq 3 : 5t \cdot [5] - 2[4] - 4[3]$
15	239	36	580	$21t - 6 \geq 36$	$341t - 102$	$t \geq 2 : 5t \cdot [5] - [4] - 4[3]$
16	256	37	597	$21t - 5 \geq 37$	$341t - 85$	$t \geq 1 : (5t-1) \cdot [5] - 4[3]$
17	273	38	614	$21t - 4 \geq 38$	$341t - 68$	$t \geq 1 : (5t-1) \cdot [5] + [2] - 4[1]$
18	290^{ilp}	39	631	$21t - 3 \geq 39$	$341t - 51$	$t \geq 3 : 5t \cdot [5] - 3[4]$
19	307^{ilp}	40	648	$21t - 2 \geq 40$	$341t - 34$	$t \geq 2 : 5t \cdot [5] - 2[4]$
20	324	41	665	$21t - 1 \geq 41$	$341t - 17$	$t \geq 1 : 5t \cdot [5] - [4]$
21	341	42	682	$21t \geq 42$	$341t$	$t \geq 1 : 5t \cdot [5]$

Table 1: Bounds for $n_4(5, 2; s)$.

Proof. The upper bound $n_4(5, 2; 2) \leq 22$ follows from Lemma 2, $n_4(5, 2; 3) \leq 42$ follows from Theorem 2, and all other upper bounds follow from the Griesmer bound. We have that $5[5]$, $[4]$, $[2]$, $[5] - [3]$, $5[5] - [4] - 4[2]$, $4[5] + [2] - 4[1]$, and $[5] + 4[1]$ are 2-partitionable over $\mathbb{F}_4$. These constructions imply that the expressions mentioned in the rightmost column of Table 1 are 2-partitionable over $\mathbb{F}_4$. For more details we refer to [19]. Here we only use those constructions for

$s \in \{4, 17, 20, 21\}$. In Section 3 we have stated an example showing $n_4(5, 2; 2) \geq 20$. Via integer linear programming computations we have found the following examples, referring to Section D in the appendix for explicit lists of generator matrices and used automorphism groups: $n_4(5, 2; 3) \geq 39$, $n_4(5, 2; 5) \geq 75$, $n_4(5, 2; 6) \geq 90$, $n_4(5, 2; 7) \geq 107$, $n_4(5, 2; 9) \geq 141$, $n_4(5, 2; 11) \geq 175$, $n_4(5, 2; 14) \geq 222$, $n_4(5, 2; 18) \geq 290$, and $n_4(5, 2; 19) \geq 307$. All other lower bounds follow from $n_q(5, 2; s_1 + s_2) \geq n_q(5, 2; s_1) + n_q(5, 2; s_2)$. $\square$

Theorem 6. *For $n_5(5, 2; s)$ we have the bounds and exact values stated in Table 2.*

Proof. The upper bounds $n_5(5, 2; 2) \leq 31$, $n_5(5, 2; 3) \leq 62$, $n_5(5, 2; 3) \leq 93$ follow from Theorem 2 and all other upper bounds follow from the Griesmer bound. We have that $6[5]$, $[4]$, $[2]$, $[5] - [3]$, $6[5] - [4] - 5[2]$, $6[5] + [2] - 5[1]$, and $[5] + 5[1]$ are 2-partitionable over $\mathbb{F}_5$. These constructions imply that the expressions mentioned in the rightmost column of Table 2 are 2-partitionable over $\mathbb{F}_5$. For more details we refer to [19]. Here we only use those constructions for $s \in \{5, 25, 26, 30, 31, 35, 60\}$. In Proposition 1 we have described a general construction showing $n_5(5, 2; 2) \geq 27$. Via integer linear programming computations we have found the following examples, referring to Section C in the appendix for explicit lists of generator matrices. Prescribing the cyclic group of order five generated by

$$\begin{pmatrix} 1 & 0 & 0 & 0 & 0 \\ 0 & 1 & 1 & 0 & 0 \\ 0 & 0 & 1 & 1 & 0 \\ 0 & 0 & 0 & 1 & 1 \\ 0 & 0 & 0 & 0 & 1 \end{pmatrix}$$

yields $n_5(5, 2; 3) \geq 50$. The cyclic group of order eleven generated by

$$\begin{pmatrix} 0 & 1 & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 0 & 1 \\ 1 & 2 & 4 & 1 & 1 \end{pmatrix}$$

gives $n_5(5, 2; 4) \geq 77$, $n_5(5, 2; 6) \geq 132$, $n_5(5, 2; 8) \geq 176$, and $n_5(5, 2; 14) \geq 330$. The cyclic group of order fifteen generated by

$$\begin{pmatrix} 1 & 0 & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 & 0 \\ 0 & 4 & 4 & 1 & 0 \\ 0 & 0 & 0 & 0 & 1 \\ 0 & 0 & 0 & 4 & 4 \end{pmatrix}$$

gives $n_5(5, 2; 7) \geq 157$, $n_5(5, 2; 11) \geq 260$, $n_5(5, 2; 16) \geq 391$, $n_5(5, 2; 17) \geq 412$, $n_5(5, 2; 21) \geq 521$, $n_5(5, 2; 22) \geq 542$, $n_5(5, 2; 37) \geq 927$, $n_5(5, 2; 39) \geq 969$, $n_5(5, 2; 44) \geq 1096$, $n_5(5, 2; 48) \geq 1203$, $n_5(5, 2; 49) \geq 1224$, $n_5(5, 2; 54) \geq 1354$,

$n_5(5, 2; 58) \geq 1458$, and $n_5(5, 2; 59) \geq 1484$. The non-commutative group of order fifty-five generated by

$$\begin{pmatrix} 0 & 0 & 0 & 0 & 1 \\ 1 & 0 & 0 & 0 & 4 \\ 0 & 1 & 0 & 0 & 4 \\ 0 & 0 & 1 & 0 & 1 \\ 0 & 0 & 0 & 1 & 3 \end{pmatrix} \quad \text{and} \quad \begin{pmatrix} 0 & 0 & 2 & 1 & 0 \\ 2 & 1 & 3 & 3 & 4 \\ 3 & 3 & 2 & 2 & 3 \\ 2 & 2 & 0 & 0 & 4 \\ 0 & 0 & 0 & 0 & 2 \end{pmatrix}$$

gives $n_5(5, 2; 12) \geq 286$, $n_5(5, 2; 13) \geq 308$, and $n_5(5, 2; 24) \geq 594$. The cyclic group of order 71 generated by

$$\begin{pmatrix} 0 & 0 & 0 & 0 & 1 \\ 1 & 0 & 0 & 0 & 3 \\ 0 & 1 & 0 & 0 & 4 \\ 0 & 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & 1 & 0 \end{pmatrix}$$

gives $n_5(5, 2; 23) \geq 568$. All other lower bounds follow from $n_q(5, 2; s_1 + s_2) \geq n_q(5, 2; s_1) + n_q(5, 2; s_2)$. $\square$

Bounds on the sizes of arcs in $\text{PG}(2, 25)$ can e.g. be found in [5].

We would like to remark that instead of searching projective systems directly using integer linear programming we can also search for linear codes or multisets of points associated to a projective system, see Lemma 1. As an example we state that

[illegible]

is the generator matrix of a 4-divisible $[350, 9, 172]_2$ code with maximum weight

s	$n_5(5, 2; s)$	s	$n_5(5, 2; s)$	s	$n_5(5, 2; s)$	construction
1	—	32	792 — 802	$31t - 30 \geq 63$	$781t - 760$	$t \geq 5 : (6t-5) \cdot [5] - 4[4] - [3]$
2	$27^{\text{P},1} - 31^{\text{T},2}$	33	818 — 828	$31t - 29 \geq 64$	$781t - 734$	$t \geq 4 : (6t-5) \cdot [5] - 3[4] - [3]$
3	$50^{\text{ilp}} - 62^{\text{T},2}$	34	844 — 854	$31t - 28 \geq 65$	$781t - 708$	$t \geq 3 : (6t-5) \cdot [5] - 2[4] - [3]$
4	$77^{\text{ilp}} - 93^{\text{T},2}$	35	880	$31t - 27 \geq 35$	$781t - 682$	$t \geq 2 : (6t-5) \cdot [5] - [4] - [3]$
5	125	36	906	$31t - 26 \geq 5$	$781t - 656$	$t \geq 1 : (6t-5) \cdot [5] - [3]$
6	$132^{\text{ilp}} - 146$	37	927^{ilp}	$31t - 25 \geq 37$	$781t - 635$	$t \geq 5 : (6t-4) \cdot [5] - 4[4] - 2[3]$
7	$157^{\text{ilp}} - 172$	38	941 — 953	$31t - 24 \geq 69$	$781t - 609$	$t \geq 4 : (6t-4) \cdot [5] - 3[4] - 2[3]$
8	$176^{\text{ilp}} - 198$	39	$969^{\text{ilp}} - 979$	$31t - 23 \geq 70$	$781t - 583$	$t \geq 3 : (6t-4) \cdot [5] - 2[4] - 2[3]$
9	202 — 224	40	1005	$31t - 22 \geq 40$	$781t - 557$	$t \geq 2 : (6t-4) \cdot [5] - [4] - 2[3]$
10	250	41	1031	$31t - 21 \geq 10$	$781t - 531$	$t \geq 1 : (6t-4) \cdot [5] - 2[3]$
11	$260^{\text{ilp}} - 271$	42	1052	$31t - 20 \geq 42$	$781t - 510$	$t \geq 5 : (6t-3) \cdot [5] - 4[4] - 3[3]$
12	$286^{\text{ilp}} - 297$	43	1067 — 1078	$31t - 19 \geq 74$	$781t - 484$	$t \geq 4 : (6t-3) \cdot [5] - 3[4] - 3[3]$
13	$308^{\text{ilp}} - 323$	44	$1096^{\text{ilp}} - 1104$	$31t - 18 \geq 75$	$781t - 458$	$t \geq 3 : (6t-3) \cdot [5] - 2[4] - 3[3]$
14	$330^{\text{ilp}} - 349$	45	1130	$31t - 17 \geq 45$	$781t - 432$	$t \geq 2 : (6t-3) \cdot [5] - [4] - 3[3]$
15	375	46	1156	$31t - 16 \geq 15$	$781t - 406$	$t \geq 1 : (6t-3) \cdot [5] - 3[3]$
16	$391^{\text{ilp}} - 396$	47	1177	$31t - 15 \geq 47$	$781t - 385$	$t \geq 5 : (6t-2) \cdot [5] - 4[4] - 4[3]$
17	$412^{\text{ilp}} - 422$	48	1203^{ilp}	$31t - 14 \geq 48$	$781t - 359$	$t \geq 4 : (6t-2) \cdot [5] - 3[4] - 4[3]$
18	433 — 448	49	$1224^{\text{ilp}} - 1229$	$31t - 13 \geq 80$	$781t - 333$	$t \geq 3 : (6t-2) \cdot [5] - 2[4] - 4[3]$
19	455 — 474	50	1255	$31t - 12 \geq 50$	$781t - 307$	$t \geq 2 : (6t-2) \cdot [5] - [4] - 4[3]$
20	500	51	1281	$31t - 11 \geq 20$	$781t - 281$	$t \geq 1 : (6t-2) \cdot [5] - 4[3]$
21	521^{ilp}	52	1302	$31t - 10 \geq 21$	$781t - 260$	$t \geq 5 : (6t-1) \cdot [5] - 4[4] - 5[3]$
22	$542^{\text{ilp}} - 547$	53	1328	$31t - 9 \geq 53$	$781t - 234$	$t \geq 4 : (6t-1) \cdot [5] - 3[4] - 5[3]$
23	$568^{\text{ilp}} - 573$	54	1354^{ilp}	$31t - 8 \geq 54$	$781t - 208$	$t \geq 3 : (6t-1) \cdot [5] - 2[4] - 5[3]$
24	$594^{\text{ilp}} - 599$	55	1380	$31t - 7 \geq 55$	$781t - 182$	$t \geq 2 : (6t-1) \cdot [5] - [4] - 5[3]$
25	625	56	1406	$31t - 6 \geq 25$	$781t - 156$	$t \geq 1 : (6t-1) \cdot [5] - 5[3]$
26	651	57	1432	$31t - 5 \geq 26$	$781t - 130$	$t \geq 1 : (6t-1) \cdot [5] + [2] - 5[1]$
27	667 — 677	58	1458^{ilp}	$31t - 4 \geq 58$	$781t - 104$	$t \geq 4 : 6t \cdot [5] - 4[4]$
28	693 — 703	59	1484^{ilp}	$31t - 3 \geq 59$	$781t - 78$	$t \geq 3 : 6t \cdot [5] - 3[4]$
29	719 — 729	60	1510	$31t - 2 \geq 60$	$781t - 52$	$t \geq 2 : 6t \cdot [5] - 2[4];$
30	755	61	1536	$31t - 1 \geq 30$	$781t - 26$	$t \geq 1 : 6t \cdot [5] - [4]$
31	781	62	1562	$31t \geq 31$	$781t$	$t \geq 1 : 5t \cdot [5]$

Table 2: Bounds for $n_5(5, 2; s)$.

200. It was found by prescribing a cyclic group of order five generated by

$$\begin{pmatrix} 1 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 1 & 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 1 & 0 & 0 & 0 & 0 \\ 0 & 1 & 1 & 1 & 1 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 1 \\ 0 & 0 & 0 & 0 & 0 & 1 & 1 & 1 & 1 \end{pmatrix}.$$

Since the corresponding multiset of points cannot be partitioned into planes, we still have $n_2(9, 3; 7) \in \{49, \dots, 55\}$, see [19, Theorem 18]. However, if $n_2(9, 3; 7) = 49$, then the upper bound cannot be deduced from the strong coding upper bound. In principle the multiset of points $\mathcal{P}(\mathcal{S})$ of a projective system $\mathcal{S}$ may have a larger automorphism group than $\mathcal{S}$ itself.

5 Multispreads in $\text{PG}(4, q)$

Multispreads are a special type of projective h -(n, k, s) $_q$ systems $\mathcal{S}$ (not necessarily faithful) that correspond to one-weight q^h -ary codes (to be exact, $\mathbb{F}_q$ -linear one-weight $[n, k/h, n-s]_{q^h}$ -codes), that is, having the property that every hyperplane includes exactly s spaces from $\mathcal{S}$. We will indicate this “exactly” by framing s with braces as follows: h -($n, k, \{s\}$) $_q$. Multispreads can be alternatively defined as follows.

Definition 8. A collection $\mathcal{S}$ of subspaces of $\mathbb{F}^k$ of dimension h is called a $(\lambda, \mu)_q^{h,k}$ -multispread if for every point (non-zero vector) v it holds

$$\sum_{S \in \mathcal{S}, v \in S} q^{h-\dim S} = \mu, \quad \sum_{S \in \mathcal{S}} (q^{h-\dim S} - 1) = \lambda,$$

i.e., every nonzero vector is covered μ times and the all-zero vector is covered $\lambda + |\mathcal{S}|$ times, where a subspace S contributes $q^{h-\dim S}$ to the multiplicity of covering.

The parameters of the projective h -($n, k, \{s\}$) $_q$ system corresponding to a $(\lambda, \mu)_q^{h,k}$ -multispread can be found from the following relations [18, Theorem 3]:

$$s = n - q^{k-h} \mu, \quad (q^h - 1)s = (q^{k-h} - 1)\mu + \lambda.$$

As shown in [18], the natural necessary condition

$$\lambda \equiv -\mu(q^k - 1) \pmod{q^h - 1}$$

is sufficient for the existence of $(\lambda, \mu)_q^{h,k}$ -multispreads for $h = 2$, $\mu \geq q$, which completely characterizes the parameters of $\mathbb{F}_q$ -linear q^2 -ary one-weight codes.

To show the same for $h = 3$ (which corresponds to $\mathbb{F}_q$ -linear q^3 -ary one-weight codes), it is sufficient, for a given prime power q , to find $q - 1$ of $(\lambda, \mu)_q^{3,5}$ multispreads that correspond to projective $3-(n, 5, \{2\})_q$ -systems, starting with $n = (q^2 + 1) + (q^3 + 1)$ ($q^2 + 1$ 2-spaces and $q^3 + 1$ 3-spaces). The next four paragraphs show what we know for $q = 2, 3, 4, 5$.

$q = 2$. Projective $3-(5+9, 5, \{2\})_2$ systems $((5, 3)_2^{3,5}$ -multispreads) were found and classified up to equivalence in [18, Appendix A.1]. The most symmetric are four multispreads with automorphism group of order 12 generated by

$$\begin{pmatrix} 1 & 0 & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 & 0 \\ 0 & 1 & 1 & 0 & 0 \\ 0 & 0 & 0 & 0 & 1 \\ 0 & 0 & 0 & 1 & 1 \end{pmatrix}, \quad \begin{pmatrix} 1 & 0 & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 & 0 \\ 0 & 1 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 1 \\ 0 & 0 & 0 & 1 & 0 \end{pmatrix}, \quad \begin{pmatrix} 1 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 0 & 1 \\ 0 & 1 & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 & 0 \end{pmatrix}.$$

$q = 3$. Projective $3-(10+28, 5, \{2\})_3$ and $3-(6+41, 5, \{2\})_3$ systems $((20, 4)_3^{3,5}$ - and $(12, 5)_3^{3,5}$ -multispreads, respectively) were found in [18, Appendix A.1]. In the current work, we classify all projective $3-(38, 5, \{2\})_3$ systems up to equivalence. The search is rather straightforward. Firstly, by adding 2-spaces one-by-one and keeping only nonequivalent collections at each step, we find all nonequivalent faithful $2-(n, 5, 2)_3$ for all n (repeating the results in [2], Table 3 ($r = 5$) and Remark 27). Then, we complete each of the 91720 $2-(10, 5, 2, 1)_3$ systems to a $3-(10, 5, \{2\})$ -system by adding $28 = 3^3$ 3-subspaces (some of them can coincide); at this step, we solve the corresponding exact covering problem (it happens that every $2-(10, 5, 2, 1)_3$ system can be completed in such a way). Although the automorphism group orders of $2-(10, 5, 2, 1)_3$ systems possess values 1 (91488 classes), 2 (169), 3 (40), 4 (2), 5 (15), 6 (4), 10 (1), 36 (1 class), a multispread can have only 1 (39857065 equivalence classes), 2 (1889), 3 (243), or 6 (15 classes) automorphisms. 14 of the last 15 multispreads have an automorphism of order 6 conjugate to $A_2 A_3$; the remaining one has an automorphism group conjugate to $\langle A_3, A'_2 \rangle \sim S_3$, where

$$A_2 = \begin{pmatrix} 2 & 0 & 0 & 0 & 0 \\ 0 & 2 & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 0 & 1 \end{pmatrix}, \quad A_3 = \begin{pmatrix} 0 & 1 & 0 & 0 & 0 \\ 2 & 2 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 1 \\ 0 & 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & 1 & 0 \end{pmatrix}, \quad A'_2 = \begin{pmatrix} 0 & 2 & 0 & 0 & 0 \\ 2 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 1 & 0 \\ 0 & 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & 0 & 1 \end{pmatrix}.$$

$q = 4$. By prescribing different automorphism groups, we have found projective $3-(17+65, 5, \{2\})_4$, $3-(12+86, 5, \{2\})_4$, $3-(7+107, 5, \{2\})_4$ systems (multispreads with parameters $(51, 5)_4^{3,5}$, $(36, 6)_4^{3,5}$, $(21, 7)_4^{3,5}$, respectively), with the full automorphism group of order 120, 40, and 7, respectively (the basis matrices are listed in Appendix B). By [18, Section 7.2], this completes the characterization of the parameters of $(\lambda, \mu)_4^{3,k}$ -multispreads and $\mathbb{F}_4$ -linear 64-ary one-weight codes.

$q = 5$. To complete the characterization of parameters of additive 5^3 -ary one-weight codes, similarly to the case $q = 4$ considered above, it is sufficient to find projective $3-(26+126, 5, \{2\})_5$, $3-(20+157, 5, \{2\})_5$, $3-(14+188, 5, \{2\})_5$, $3-(8+219, 5, \{2\})_5$ systems $((104, 6)_5^{(3,5)-}$, $(80, 7)_5^{(3,5)-}$, $(56, 8)_5^{(3,5)-}$, $(32, 9)_5^{(3,5)-}$ -multispreads. The last 3 types of systems are relatively easy to find. We first

search for faithful $2-(n, 5, 2, 1)_5$ systems, $n = 8, 14, 20$, respectively, with the prescribed automorphism group of order six generated by

$$\begin{pmatrix} 0 & 1 & 0 & 0 & 0 \\ 1 & 4 & 0 & 0 & 0 \\ 0 & 0 & 0 & 1 & 0 \\ 0 & 0 & 1 & 4 & 0 \\ 0 & 0 & 0 & 0 & 1 \end{pmatrix}, \quad \begin{pmatrix} 0 & 1 & 0 & 0 & 0 \\ 1 & 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 1 & 0 \\ 0 & 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & 0 & 1 \end{pmatrix}.$$

In each case, one of the first several solutions is extendable to a required multispread (see examples in Appendix B). However, we have not succeeded in finding a projective $3-(26+126, 5, \{2\})_5$ system. By prescribing different automorphism groups of order at least 4, we have found thousands of faithful $2-(26, 5, 2, 1)_5$ system from only 4 equivalence classes. No one of them can be completed to a multispread. We conjecture that if a projective $3-(26+126, 5, \{2\})_5$ system exists, then it has at most 3 automorphisms. If it does not exist, then the following multispreads cannot be constructed recursively and should be considered separately:

- Next λ : a $(228, 6)_5^{3,5}$ -multispread (projective $3-(57+96, 5, 3)_5$ system).
- Next k : a $(104, 6)_5^{3,8}$ -multispread (projective $3-(26+18876, 5, 152)_5$ system).

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A An alternative construction for sets of subspaces with at most two in each hyperplane

Here we give an alternative construction of projective $2-(q^2, 5, 2)_q$ systems, for the special case when the field size q is an odd prime. Although the construction gives systems (and codes) equivalent to those constructed in Section 3 in more general settings, the approach is completely different, and we believe it is of independent interests, as a rare example of a non-computational construction of a code with prescribed automorphism group. Based on this we give an alternative proof of Proposition 4 for the case $l = s = 2$.

For an odd prime q , we will construct a faithful $2-(q^2 + 2, 5, 2)_q$ system with a prescribed automorphism group generated by the following two matrices (only non-zero elements are shown, where α is a non-square in $\mathbb{F}_q$):

$$A = \begin{array}{c} \begin{array}{ccccc} 1 & \xrightarrow{\text{blue}} & 1 & & \\ & \downarrow \text{blue} & & & \\ & 1 & \xrightarrow{\text{green}} & 1 & \\ & & \downarrow \text{green} & & \\ & & 1 & \xrightarrow{\text{blue}} & 1 \\ & & & \downarrow \text{green} & \\ & & & 1 & \\ & & & & \downarrow \text{blue} \\ & & & & 1 \end{array} \\ A = \end{array} \quad A' = \begin{array}{c} \begin{array}{ccccc} 1 & \xrightarrow{\text{blue}} & \alpha & & \\ & \downarrow \text{blue} & & & \\ & 1 & \xrightarrow{\text{green}} & 1 & \\ & & \downarrow \text{green} & & \\ & & 1 & \xrightarrow{\text{blue}} & 1 \\ & & & \downarrow \text{green} & \\ & & & 1 & \\ & & & & \downarrow \text{blue} \\ & & & & 1 \end{array} \\ A' = \end{array} \quad (4)$$

These matrices commute and each of them has order q as a group element, which can be seen from the proof of the following lemma.

Lemma 4. In $\text{PG}(4, q)$, where q is an odd prime, consider q^4 lines with generator matrices of the form

$$\begin{bmatrix} 1 & 0 & x & y & z \\ 0 & 1 & x' & y' & z' \end{bmatrix}, \quad \text{where } x - y' = \frac{1}{2}, \quad y - \alpha x' = \frac{\alpha}{2}. \quad (5)$$

(i) All these q^4 lines are disjoint to the 3-space

$$S = \langle (0, 0, 0, 0, 1), (0, 0, 0, 1, 0), (0, 0, 1, 0, 0) \rangle.$$

(ii) The set of these q^4 lines is partitioned into q^2 orbits under $\langle A, A' \rangle$, where each orbit is a faithful projective $2-(q^2, 5, 2, 1)_q$ system.

(iii) Moreover, the affine span of the generator matrices, in the form (5), of each of the q^2 orbits coincides with the 4-dimensional affine space of all matrices defined by equations (5).

Proof. The action of A and A' on subspaces with generator matrix of the form in Equation (5) is the following:

$$A^i : \begin{bmatrix} 1 & 0 & x & y & z \\ 0 & 1 & x' & y' & z' \end{bmatrix} \rightarrow \begin{bmatrix} 1 & 0 & x+i & y & z+xi + \binom{i}{2} \\ 0 & 1 & x' & y'+i & z'+x'i \end{bmatrix}, \quad (6)$$

$$A'^j : \begin{bmatrix} 1 & 0 & x & y & z \\ 0 & 1 & x' & y' & z' \end{bmatrix} \rightarrow \begin{bmatrix} 1 & 0 & x & y+\alpha j & z+yj + \alpha \binom{j}{2} \\ 0 & 1 & x'+j & y' & z'+y'j \end{bmatrix}, \quad (7)$$

$$\begin{aligned} A^i A'^j : \begin{bmatrix} 1 & 0 & x & y & z \\ 0 & 1 & x' & y' & z' \end{bmatrix} \\ \rightarrow \begin{bmatrix} 1 & 0 & x+i & y+\alpha j & z+ix+jy + \binom{i}{2} + \alpha \binom{j}{2} \\ 0 & 1 & x'+j & y'+i & z'+ix'+jy' + \underline{ij} \end{bmatrix}. \end{aligned} \quad (8)$$

We start with two auxiliary statements.

(a) If a line (to be exact, its generator matrix in form (5)) belongs the 4-dimensional affine subspace defined by equations (5), then the same is true for all lines from its orbit. Indeed, as we see from (8), the transform $A^i A'^j$ keeps the differences $x - y'$ and $y - \alpha x'$.

(b) The span of the generator matrices in form (5) of the subspaces of an orbit (of one of subspaces in such form) is a 4-dimensional affine space. From the argument in (a) we see that the dimension is at most 4. For a matrix M defined as in (5), the three matrices M , MA , and MA' generate a 2-dimensional affine space of matrices of form (8) without the underlined parts. The matrices MA^2 and MAA' have form (8) with nonzero underlined part and add two more dimensions. So, the affine span of M , MA , MA' , MA^2 , MAA' has dimension 4.

Next, we want to find x, y, z, x', y', z' such that all q^2 subspaces spanned by the last matrix for different i, j are mutually disjoint (actually, this condition

holds automatically if the next one holds¹) and, moreover, every hyperplane includes at most two of them (i.e., every three of them span the whole space).

The last condition is equivalent to the fact that the dual 3-subspaces $T_{i,j}^\perp$ generated by

$$M_{i,j} = \begin{bmatrix} x+i & x'+j & -1 & 0 & 0 \\ y+\alpha j & y'+i & 0 & -1 & 0 \\ z+ix+jy+\binom{i}{2}+\alpha\binom{j}{2} & z'+ix'+jy'+ij & 0 & 0 & -1 \end{bmatrix} \quad (9)$$

covers each point with multiplicity 0, 1, or 2. It is sufficient to check that every point in $T_{0,0}^\perp$ belongs to at most one other $T_{i,j}^\perp$. Note that if $T_{0,0}^\perp$ and $T_{i,j}^\perp$ have a common vector $v = (v, v', u, u', u'')$, then it is the linear combination of the rows of each of $M_{0,0}$, $M_{i,j}$ with the same coefficients $-u, -u', -u''$: $v = (-u, -u', -u'')M_{0,0} = (-u, -u', -u'')M_{i,j}$.

Clearly, the first or the second rows of $M_{0,0}$ and $M_{i,j}$, where $(i, j) \neq (0, 0)$, cannot coincide (recall that x, y, z, x', y' , and z' are fixed). Let us check the case when a linear combination of the first two rows, with coefficients 1 and $k \neq 0$, coincides. We have

$$\begin{cases} x+i+k(y+\alpha j) &= x+ky \\ x'+j+k(y'+i) &= x'+ky' \end{cases},$$

$$\begin{cases} i+k\alpha j = 0 \\ ki+j = 0 \end{cases}.$$

The last system has a non-zero solution only if $\alpha = k^{-2}$, which is impossible because α is not a square. Hence, the corresponding points are covered only once, for any x, y, x', y' (and, of course, for any z, z'). Linear combinations including the last row are considered differently because the system becomes non-linear in i, j . We consider only orbits with the representatives $x = -x' = \frac{1}{2}$, $y = y' = 0$, z and z' arbitrary. In particular,

$$M_{i,j} = \begin{bmatrix} \frac{1}{2}+i & -\frac{1}{2}+j & -1 & 0 & 0 \\ \alpha j & i & 0 & -1 & 0 \\ z+\frac{i}{2}+\binom{i}{2}+\alpha\binom{j}{2} & z'-\frac{i}{2}+ij & 0 & 0 & -1 \end{bmatrix}.$$

For these values, the linear combinations of the rows with coefficients $k, l, 1$ coincide for $M_{0,0}$ and $M_{i,j}$ if and only if

$$\begin{cases} ki+l\alpha j+\frac{i}{2}+\binom{i}{2}+\alpha\binom{j}{2} = 0 \\ kj+li-\frac{i}{2}+ij = 0 \end{cases},$$

$$\begin{cases} i^2+2ki+\alpha j^2+2L\alpha j = 0 \\ kj+Li+ij = 0 \end{cases}, \quad \text{where } L = l - \frac{1}{2}.$$

¹If a line T from the system intersects with $T' = A^i A'^j T$, then it intersects with $T'' = A^{-i} A'^{-j} T$; among $q^2 + q + 1$ hyperplanes including T , $2q + 2$ include T' or T'' ; the remaining $q^2 - q - 1$ hyperplanes include the remaining $q^2 - 3$ system lines, which means that some hyperplanes includes more that two system lines, a contradiction.

If $k = 0$ and $L = 0$, we have no non-zero solutions. If $k = 0$ and $L \neq 0$, then either $i = 0$ and we have two solutions for j (0 and $-2L$) or $j = -L$ and $i^2 - L^2\alpha = 0$, which has no solutions because α is not a square.

Similarly, if $k \neq 0$ and $L = 0$, then either $j = 0$ and we have two solutions for i (0 and $-2k$) or $i = -k$ and $\alpha j^2 = k^2$, which has no solutions because α is not a square.

If $k \neq 0$ and $L \neq 0$, we have

$$\begin{cases} (i+k)^2 + \alpha(j+L)^2 = k^2 + \alpha L^2 \\ (i+k)(j+l) = kL \end{cases},$$

$$\begin{cases} I^2 + \alpha J^2 = K^2 + \alpha \\ IJ = 1 \end{cases}, \quad \text{where } K = \frac{k}{L}, \quad I = \frac{i+k}{L}, \quad J = \frac{j+L}{L},$$

$$X^2 - (K^2 + \alpha)X + \alpha, \quad \text{where } X = I^2.$$

If the last quadratic equation in X has two solutions, then one of them is square and one non-square because their product is the non-square α . Hence, only one of them is resolvable in I , and we have only two solutions for (i, j) . We know one of them is $(0, 0)$, and we can easily find the other.

We have proved that

(c) for any z, z' , the orbit of the line with generator matrix $\begin{bmatrix} 1 & 0 & \frac{1}{2} & 0 & z \\ 0 & 1 & -\frac{1}{2} & 0 & z' \end{bmatrix}$

is a faithful $2 - (q^2, 5, 2, 1)_q$ system.

From (8), it is easy to see that all these q^2 orbits are different. Combining claims (a), (b), (c) completes the proof. $\square$

We remark that experiments with small q show that other orbits under $\langle A, A' \rangle$ do not give $2 - (q^2, 5, 2)_q$ systems.

Theorem 7. *For any odd prime q , there is a faithful $2 - (q^2 + 2, 5, 2)_q$ system (and hence, an additive $[q^2 + 2, 2.5, q^2]_{q^2}$ code) invariant under the actions of A, A' defined in (4).*

Proof. We will add two more lines to the faithful projective $2 - (q^2, 5, 2)_q$ system C constructed in Lemma 4. One of them is the 2-space D generated by $\begin{pmatrix} 0 & 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 0 & 1 \end{pmatrix}$. To ensure that we can add it, we need to check that every point from the dual space $D^\perp$, with basis $\begin{pmatrix} 1 & 0 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 & 0 \end{pmatrix}$, belongs to only one $T_{i,j}^\perp$. This is obvious from the basis matrix (9) of $T_{i,j}^\perp$. Moreover, this point can only be the first line of (9).

The same arguments work for the line D' generated by $\begin{pmatrix} 0 & 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & 0 & 1 \end{pmatrix}$, with intersecting points of dual 3-subspaces coinciding with the second line of (9).

Since the common points of $D^\perp$ and $D'^\perp$ do not belong to any $T_{i,j}^\perp$, we can add both D and D' to get a faithful projective $2 - (q^2 + 2, 5, 2)_q$ system. Finally, it is easy to see that $DA = DA' = D$ and $D'A = D'A' = D'$, i.e., adding D and D' keeps the system $\langle A, A' \rangle$ -invariant. $\square$

Remark 1. (i) Actually, there are $q + 1$ $\langle A, A' \rangle$ -invariant lines, D and q lines with basis matrix of the form $\begin{pmatrix} 0 & 0 & 1 & y & 0 \\ 0 & 0 & 0 & 0 & 1 \end{pmatrix}$. So, any two of them can be chosen as the two added extra lines. Different choices can result in non-equivalent systems and additive codes. (ii) Since D and D' intersect, the resulting projective system does not have parameters $2 - (q^2 + 2, 5, 2, 1)_q$. However, by adding only one of them, we get a faithful projective $2 - (q^2 + 1, 5, 2, 1)_q$ system.

B Examples of multispreads

Here, we list examples of projective systems corresponding to one-weight codes with new parameters. The elements of $\mathbb{F}_4$ are denoted 0, 1, ω , $v = \omega^2$.

A projective $3-(82, 5, !2)_4$ system, i.e., a $(51, 5)_4^{3,5}$ -multispread:

$(1001\omega), (0110\omega), (1\omega000), (1v000), (100\omega1), (10\omega\omega1), (10000), (10v\omega1), (101\omega1), (10100),$
 $(00100), (00010), (001\omega0), (001v0), (01000), (01\omega01), (01\omega01), (01\omega v1), (01010), (01\omega11),$
 $(10\omega vv), (10\omega00), (101vv), (10v00), (100vv), (10vvv), (01\omega00), (01010), (1000v), (1000\omega),$
 $(010\omega0), (01v\omega v), (01v1v), (01vvv), (01v0v), (010v0), (00001), (001v\omega), (001\omega v), (0001v),$

$(1\omega00v), (0100\omega), (0100v), (0100\omega), (0100v), (0100\omega), (0100v), (0100\omega), (0100v), (0100\omega),$
 $(0011v), (0011\omega), (0011v), (0011\omega), (0011v), (0011\omega), (0011v), (0011\omega), (0011v), (0011\omega),$
 $(1000v), (1000\omega), (1000v), (1000\omega), (1000v), (1000\omega), (1000v), (1000\omega), (1000v), (1000\omega),$
 $(010\omega1), (010v1), (010\omega v), (010v\omega), (010\omega v), (010v\omega), (010\omega v), (010v\omega), (010\omega v), (010v\omega),$
 $(001\omega1), (001v\omega), (001\omega v), (001v\omega), (001\omega v), (001v\omega), (001\omega v), (001v\omega), (001\omega v), (001v\omega),$
 $(100\omega\omega), (10011), (1000\omega), (1001v), (100v0), (100\omega1), (1001v), (10001), (100v1), (100\omega v),$
 $(010\omega1), (010v1), (010\omega v), (010v\omega), (010\omega v), (010v\omega), (010\omega v), (010v\omega), (010\omega v), (010v\omega),$
 $(001\omega1), (001v\omega), (001\omega v), (001v\omega), (001\omega v), (001v\omega), (001\omega v), (001v\omega), (001\omega v), (001v\omega),$
 $(100\omega v), (10010), (10010), (1001v), (100v1), (100vv), (1000v), (10001), (100v1), (100\omega v),$
 $(010\omega v), (01011), (0101v), (010\omega1), (010v1), (010vv), (0100v), (01000), (010v1), (010\omega v),$
 $(001vv), (0010\omega), (001vv), (001v1), (001\omega\omega), (0010\omega), (0001\omega), (0001v), (0010\omega), (0001v),$
 $(100v0), (1000v), (10011), (100v\omega), (100v0), (100\omega0), (1000\omega), (100v\omega), (100v0), (100\omega0),$
 $(010\omega v), (010v\omega), (010\omega v), (010v\omega), (010\omega v), (010v\omega), (010\omega v), (010v\omega), (010\omega v), (010v\omega),$
 $(001\omega v), (0010\omega), (001\omega v), (0010\omega), (001\omega v), (0010\omega), (001\omega v), (0010\omega), (001\omega v), (0010\omega),$
 $(100vv\omega), (10\omega0v), (10001), (10000), (10100), (10\omega\omega0), (10v\omega0), (011\omega0), (011v0), (011\omega0),$
 $(0101v), (0101\omega), (0100\omega), (010v1), (00001), (00001), (00001), (00001), (00001), (00001).$

A projective $3-(98, 5, !2)_4$ system, i.e., a $(36, 6)_4^{3,5}$ -multispread:

$(110vv), (100vv), (1011\omega), (10000), (1001\omega), (10v\omega1), (101\omega1), (10100), (10\omega\omega1), (10\omega00),$
 $(00110), (00100), (0111\omega), (0110\omega), (01000), (01\omega v1), (01010), (01\omega11), (010\omega0), (01\omega\omega1),$
 $(100\omega1), (100\omega\omega), (10v01), (1000v), (100\omega\omega), (10001), (1010\omega), (10\omega0\omega), (100\omega\omega),$
 $(01\omega01), (010\omega1), (01\omega0\omega), (01000), (010\omega1), (01001), (01001), (01\omega01), (010\omega1),$
 $(100v1), (100\omega\omega), (1001v), (10001), (1001v), (1100\omega), (100v\omega), (1000v), (10\omega01),$
 $(0100v), (00101), (0101\omega), (0101\omega), (0100v), (00101), (0101\omega), (0100v), (0100v),$
 $(00111), (100\omega0), (100\omega1), (100v0), (1000\omega), (100v1), (100\omega1), (100vv), (10\omega0v),$
 $(010\omega1), (0101\omega), (0100v), (010vv), (01000), (0101\omega), (01000), (0100v), (01\omega0v),$
 $(001v1), (00111), (0010\omega), (00101), (00010), (001\omega0), (00111), (00101), (00011),$
 $(100v0), (1000v), (10011), (100v\omega), (1v0\omega0), (1\omega0\omega0), (1000\omega), (100v\omega), (1v00v),$
 $(01010), (010\omega0), (010vv), (010\omega1), (001\omega0), (001v0), (010vv), (010\omega v), (00101),$
 $(0010\omega), (0010\omega), (001v0), (0010v), (00001), (00001), (001\omega\omega), (001\omega\omega), (0001\omega),$
 $(100\omega v), (1001v), (10010), (100v\omega), (100\omega0), (1000\omega), (1\omega00\omega), (10001), (100v1),$
 $(01001), (01011), (010\omega\omega), (010vv), (0100\omega), (0101v), (00101), (010v0), (010v0),$
 $(001\omega\omega), (001\omega\omega), (001vv), (001vv), (001vv), (001vv), (001vv), (001\omega\omega), (0011\omega),$
 $(10v00), (100\omega0), (10010), (100\omega v), (10v01), (10000), (1001v), (100vv), (10100),$
 $(01001), (010v0), (010v0), (010v1), (0100\omega), (010v\omega), (010v\omega), (010v1), (01110),$
 $(0001\omega), (001v0), (001\omega0), (001v0), (0001v), (00100), (001\omega0), (0011v), (00001),$
 $(10000), (10\omega10), (10v10), (100v0), (10\omega0v), (10010), (1000v), (100\omega v), (100v0),$
 $(01v00), (011\omega0), (011\omega0), (010\omega\omega), (01101), (010vv), (010vv), (0100\omega), (0101v),$
 $(00001), (00001), (00001), (0001v), (0001v), (0001v), (001\omega v), (001\omega v), (001\omega v),$
 $(100\omega0), (1000v), (10v0\omega), (1001v), (1001\omega), (10001), (1001v), (100\omega v), (100\omega0),$
 $(010vv), (01001), (01100), (010\omega\omega), (0100\omega), (0100\omega), (0101v), (0101v), (01011),$
 $(0011\omega), (001v1), (0001v), (0010v), (0010v), (001\omega v), (001\omega v), (001\omega v), (001v1),$
 $(10v0v), (10011), (1000v), (1010v), (1010v), (10011), (10101), (10101), (1000\omega),$
 $(01v01), (01\omega01), (01001), (010v1), (01\omega0v), (010v1), (010vv), (01v01), (010\omega\omega),$
 $(10010), (10011), (100v1), (10001), (100v0), (100v1), (100v1), (100v1), (100v1),$
 $(01011), (01011), (0101v), (010v1), (010v1), (010v1), (010v1), (010v1), (010v1),$
 $(001v\omega), (0010v), (001\omega1), (001v1), (001\omega1), (0011v), (0011v), (0011v), (0011v),$

A projective $3-(114, 5, !2)_4$ system, i.e., a $(21, 7)_4^{3,7}$ -multispread, with pre-

$$\begin{array}{l}
\text{scribed automorphism} \begin{bmatrix} 00100 \\ 10000 \\ 01100 \\ 00010 \\ 00001 \end{bmatrix} : \quad (010\omega\omega)^7, (100\omega0), (1100\omega), (1000\omega), (101\omega0), \\
(100\omega\omega), (1010\omega), (01010)^7, (10010), (11000), (10000), (10110), (10010), (10100), \\
(1\omega00\omega)^7, (10\omega01), (10\omega01), (1000v), (1010v), (10\omega00), (10\omega01), (1\omega00\omega)^7, (10\omega00), \\
(0010v), (0100v), (0110v), (01\omega0v), (01\omega00), (01\omega0v), (01v0\omega), (00101), (01001), \\
(10v01), (10001), (10101), (10\omega0v), (10\omega0v), (1v00v)^7, (10v0v), (10\omega01), (10v00), \\
(01101), (01\omega00), (01\omega00), (01\omega0\omega), (01v0\omega), (0010v), (0100v), (0110v), (01\omega0v), \\
(00011), (00011), (00011), (00011), (00011), (00011), (00011), (00011), (00011), \\
(1000v), (1010v), (10v0v), (1v000)^7, (10v01), (10\omega00), (10v0v), (1000v), (1010v), \\
(01v01), (01v01), (01v00), (0010v), (0100v), (0110v), (01\omega00), (0001v), (0001v), \\
(0001\omega), (0001\omega), (0001\omega), (0001v), (0001v), (0001v), (0001v), (0001v), (0001v), \\
(10v0\omega), (10000)^1, (10000)^1, (100v0)^7, (10001), (100v1), (10001), (10001), (10000), \\
(01v01), (01000), (01000), (01000), (010v0), (010v0), (01001), (01001), (010v1), \\
(001v1), (001v1), (001v1), (001v1), (001v1), (001v1), (001v1), (001v1), (001v1), \\
(100v0), (100vv)^7, (1000v), (100v0), (10000), (100vv), (1000v), (100v0), (100v0), \\
(010v1), (010v1), (010v1), (010v1), (010v1), (010v1), (010v1), (010v1), (010v1), \\
(1000\omega), (100\omega v), (1001\omega), (100vv), (10010), (100v1), (100v1)^7, (100v0), (10001), \\
(010\omega1), (010\omega v), (010\omega v), (010v1), (010v1), (010v1), (010v1), (010v1), (010v1), \\
(00110), (0011\omega), (001\omega1), (001\omega v), (001\omega v), (001\omega v), (001\omega v), (001\omega v), (001\omega v), \\
(1001v), (1001v), (1001v), (1001v), (1001v), (1001v), (1001v), (1001v), (1001v), \\
(01001), (0101v), (010\omega\omega), (010v0), (01011), (010v0), (010v0), (010v0), (010v0), \\
(001\omega\omega), (001\omega v), (001v0), (001v0), (001v1), (001v1), (001v1), (001v1), (001v1), \\
(100\omega v), (10011), (1001v)^7, (100\omega0), (100vv), (10001), (1001\omega), (100\omega1), (100\omega v), \\
(010\omega1), (010v0), (010\omega0), (0101\omega), (010v\omega), (0101v), (010v1), (010v1), (010v1), \\
(001v0), (001v\omega), (00101), (0011v), (0011\omega), (0011\omega), (001\omega1), (001\omega0), (001v\omega), \\
(100v1)^7, (100\omega1), (10010), (100v1), (10000), (10010), (100\omega1), (100vv)^7, (100\omega v), \\
(010\omega1), (010\omega1), (010\omega1), (010\omega1), (010v1), (010v1), (010v1), (010v1), (010v1), \\
(00100), (00110), (00110), (001\omega1), (001\omega1), (001\omega1), (001v1), (001v1), (001v1), \\
(10011), (100vv), (10000), (10011), (100\omega v), (10011)^7, (100vv), (100\omega\omega), (100v0), \\
(010\omega v), (01011), (010vv), (01011), (010vv), (010vv), (010v1), (010\omega1), (010v0), \\
(00111), (001\omega v), (001\omega v), (001\omega v), (001\omega v), (001\omega v), (0011\omega), (0011\omega), (0011\omega), \\
(100\omega1), (1000v), (1001\omega), (100\omega0)^7, (100vv), (1001v), (1001v), (100vv), (100\omega1), \\
(010v0), (010\omega\omega), (01011), (010v0), (010v1), (010v1), (010v1), (010v1), (010v1), \\
(001\omega\omega), (001v0), (001vv), (00101), (0011v), (0011\omega), (001\omega1), (001\omega0), (001vv), \\
(10001), \\
(010\omega0), \\
(001vv).
\end{array}$$

A projective 3-(177, 5, !2)₅ system, i.e., a (80, 7)₅^{3,5}-multispread, with pre-

$$\begin{array}{l}
\text{scribed automorphisms} \begin{bmatrix} 10000 \\ 00100 \\ 04400 \\ 00001 \\ 00044 \end{bmatrix}, \begin{bmatrix} 10000 \\ 00100 \\ 01000 \\ 00001 \\ 00010 \end{bmatrix} : \quad (01003)^2, (01022), (10231)^6, (10223), (10322), \\
(10330), (12013), (13022), (10243)^6, (10214), (10324), (10332), (12034), (13042), (10311)^6, \\
(01101), (00111), (00140), (01024), (01123), (01031), (01132), (00142), (00113), (01310), \\
(10340), (10410), (10443), (10414), (10444), (10000)^1, (10001)^3, (10003), (10003), (10003)^3, \\
(01311), (01202), (01222), (01420), (01403), (00010), (00102), (01001), (01104), (01002), \\
(10022), (10030), (10004)^3, (10011), (10040), (10002)^6, (10002), (10020), (10020), \\
(01011), (01020), (01001), (01044), (01030), (01001), (01032), (01003), (01022), \\
(00111), (00140), (00103), (00144), (00110), (00130), (00122), (00110), (00123), \\
(10033), (10033), (10004)^6, (10004), (10011), (10011), (10040), (10040), (10001)^3, \\
(01013), (01044), (01000), (01030), (01000), (01030), (01002), (01033), (01014), \\
(00144), (00131), (00133), (00120), (00103), (00100), (00103), (00100), (00103), \\
(10010), (10044), (10004)^3, (10011), (10040), (10000)^2, (10000), (10002)^6, (10002), \\
(01030), (01021), (01014), (01021), (01030), (01014), (01012), (01010), (01034), \\
(00141), (00112), (00103), (00112), (00141), (00112), (00141), (00124), (00132), \\
(10020), (10020), (10033), (10033), (10000)^2, (10000), (10000)^2, (10000), (10001)^3, \\
(01023), (01042), (01010), (01041), (01012), (01012), (01043), (01012), (01023), \\
(00143), (00101), (00114), (00101), (00134), (00121), (00134), (00121), (00101), \\
(10010), (10044), (10002)^6, (10002), (10020), (10020), (10033), (10033), (10004)^6, \\
(01010), (01042), (01020), (01033), (01001), (01044), (01002), (01020), (01022), \\
(00132), (00124), (00110), (00144), (00102), (00133), (00102), (00120), (00120), \\
(10004), (10011), (10011), (10040), (10040), (10001)^3, (10010), (10044), (10001)^3, \\
(01042), (01003), (01023), (01002), (01033), (01034), (01000), (01041), (01040), \\
(00133), (00132), (00130), (00122), (00124), (00100), (00143), (00114), (00104), \\
(10010), (10044), (10003)^3, (10022), (10030), (10013)^6, (10024), (10023), (10032), \\
(01040), (01040), (01041), (01034), (01020), (01000), (01014), (01021), (01000), \\
(00104), (00104), (00102), (00143), (00114), (00112), (00141), (00100), (00112), \\
(10031), (10042), (10013)^6, (10023), (10024), (10031), (10032), (10042), (10013)^6, \\
(01021), (01014), (01002), (01002), (01002), (01033), (01033), (01033), (01004), \\
(00100), (00141), (00133), (00133), (00133), (00133), (00120), (00120), (00120), \\
(10023), (10024), (10031), (10042), (10014)^6, (10012), (10012), (10012), (10034), \\
(01001), (01021), (01011), (01014), (01044), (01012), (01032), (01043), (01010), \\
(00111), (00144), (00110), (00140), (00112), (00101), (00134), (00123), (00131),
\end{array}$$

A projective 3-(202, 5, 12) ₅ system, i.e., a (56, 8) ₅ ^{3,5} -multispread:										(1002) ² (10133),
(01033) (00120),	(10110) ⁶ (01004),	(10144) (01101),	(10421) (01013) ³ ,	(10434) (01110),	(11001) (00140),	(14012) (00111),	(10114) ⁶ (01023),	(10143) (01124),	(10143) (01042),	(10133),
(10442) (01142),	(11041) (00132),	(14031) (00124),	(10001) ³ (01012),	(10003) (01001),	(10003) (01104),	(10001) ³ (00102),	(10003) (01001),	(10003) (01104),	(10002) (01001),	(10002) (00102),
(10002) (01002) (00102),	(10020) (01020) (00110),	(10020) (01020) (00120),	(10033) (01033) (00144),	(10033) (01044) (00133),	(10002) ⁶ (01000) (00112),	(10002) (01014) (00141),	(10020) (01014) (00141),	(10020) (01014) (00141),	(10020) (01021) (00100),	(10020) (01021) (00100),
(10033) (01000) (00112),	(10033) (01021) (00100),	(10000) ² (01003) (00122),	(10000) (01022) (00130),	(10004) ⁶ (01001) (00130),	(10004) (01032) (00122),	(10011) (01013) (00144),	(10011) (01013) (00144),	(10011) (01044) (00131),	(10040) (01003) (00110),	(10040) (01003) (00110),
(10040) (01022) (00123),	(10002) ⁶ (01001) (00142),	(10002) (01041) (00113),	(10020) (01024) (00110),	(10020) (01031) (00114),	(10033) (01034) (00144),	(10033) (01044) (00143),	(10001) ³ (01014) (00103),	(10010) (01030) (00141),	(10010) (01030) (00141),	(10010) (01030) (00141),
(10044) (01021) (00112),	(10000) ² (01014) (00112),	(10000) (01021) (00141),	(10003) ⁶ (01012) (00114),	(10003) (01021) (00143),	(10022) (01014) (00134),	(10022) (01043) (00141),	(10030) (01034) (00112),	(10030) (01041) (00112),	(10030) (01041) (00121),	(10030) (01041) (00121),
(10000) ² (01013) (00123),	(10000) (01032) (00131),	(10002) ⁶ (01010) (00122),	(10002) (01031) (00130),	(10020) (01003) (00113),	(10020) (01022) (00101),	(10033) (01010) (00142),	(10033) (01024) (00101),	(10033) (01011) (00101),	(10033) (01011) (00101),	(10033) (01011) (00101),
(10003) (01040) (00120),	(10022) (01004) (00104),	(10022) (01040) (00140),	(10030) (01002) (00104),	(10030) (01033) (00111),	(10004) ³ (01022) (00103),	(10011) (01003) (00130),	(10040) (01030) (00122),	(10004) ⁶ (01020) (00111),	(10004) ⁶ (01020) (00111),	(10004) ⁶ (01020) (00111),
(10004) (01032) (00140),	(10011) (01013) (00102),	(10011) (01020) (00131),	(10040) (01004) (00123),	(10040) (01011) (00102),	(10001) ⁶ (01022) (00121),	(10001) (01041) (00134),	(10010) (01012) (00122),	(10010) (01043) (00114),	(10010) (01043) (00114),	(10010) (01043) (00114),
(10044) (01003) (00143),	(10044) (01034) (00130),	(10001) ³ (01030) (00103),	(10010) (01030) (00103),	(10044) (01030) (00103),	(10000) ² (01034) (00114),	(10000) (01041) (00143),	(10004) ³ (01043) (00103),	(10011) (01012) (00121),	(10011) (01012) (00121),	(10011) (01012) (00121),
(10040) (01030) (00134),	(10013) ⁶ (01000) (00123),	(10024) (01013) (00142),	(10023) (01031) (00100),	(10032) (01000) (00113),	(10031) (01032) (00100),	(10042) (01024) (00131),	(10014) ⁶ (01000) (00121),	(10012) (01014) (00100),	(10012) (01014) (00100),	(10012) (01014) (00100),
(10021) (01000) (00141),	(10034) (01043) (00112),	(10041) (01012) (00100),	(10043) (01021) (00134),	(10014) ⁶ (01001) (00141),	(10012) (01023) (00144),	(10021) (01044) (00132),	(10034) (01021) (00124),	(10041) (01014) (00110),	(10041) (01014) (00110),	(10041) (01014) (00110),
(10043) (01042) (00112),	(10013) ⁶ (01010) (00110),	(10023) (0								

A projective 3-(227, 5, 12) ₅ system, i.e., a (32, 9) ₅ ^{3,5} -multispread:										(01013) ₅ ² (00123) ₅
(01032) (00131),	(10141) ³ (01212),	(10112) (01414),	(10201) (01313),	(10302) ³ (01334),	(10432) (01231),	(10424) (01432),	(10003) ³ (00100, 00013),	(10004) (01000, 00012),	(10004) (01100, 00014),	
(10004) ³ (00100, 00013),	(10002) (01000, 00012),	(10002) (01000, 00014),	(10002) ³ (01001, 000103),	(10020) (01030, 00110),	(10033) (01044, 00144),	(10002) ³ (01004, 00102),	(10020) (01020, 00140),	(10033) (01011, 00111),		
(10001) ⁶ (01002, 00110),	(10001) (01014, 00144),	(10010) (01001, 00120),	(10010) (01044, 00141),	(10044) (01021, 00133),	(10044) (01033, 00112),	(10000) ² (01003, 00122),	(10000) (01022, 00130),	(10003) ⁶ (01001, 00130),		
(10003) (01032, 00122),	(10022) (01013, 00144),	(10022) (01044, 00131),	(10030) (01003, 00110),	(10030) (01022, 00123),	(10004) ⁶ (01004, 00132),	(10004) (01032, 00124),	(10011) (01013, 00111),	(10011) (01011, 00131),		
(10040) (01023, 00140),	(10040) (01042, 00123),	(10001) ⁶ (01001, 00141),	(10001) (01042, 00112),	(10010) (01014, 00110),	(10010) (01021, 00124),	(10044) (01023, 00144),	(10044) (01032, 00132),	(10001) ⁶ (01004, 00143),		
(10001) (01042, 00114),	(10010) (01034, 00140),	(10010) (01041, 00124),	(10044) (01011, 00132),	(10044) (01023, 00111),	(10000) ¹ (01010, 00101),	(10000) ⁶ (01014, 00114),	(10000) (01021, 00113),	(10000) (01024, 00143),		
(10000) (01031, 00112),	(10000) (01034, 00142),	(10000) (01041, 00141),	(10002) ⁶ (01014, 00113),	(10002) (01020, 00142),	(10020) (01024, 00102),	(10020) (01031, 00141),	(10033) (01021, 00102),	(10033) (01020, 00112),		
(10004) (01011, 00133),	(10004) (01040, 00120),	(10011) (01004, 00104),	(10011) (01040, 00140),	(10040) (01002, 00104),	(10040) (01033, 00111),	(10002) ³ (01021, 00100),	(10020) (01000, 00112),	(10033) (01014, 00141),		
(10001) ⁶ (01022, 00121),	(10001) (01041, 00134),	(10010) (01012, 00122),	(10010) (01043, 00114),	(10044) (01003, 00143),	(10044) (01034, 00130),	(10004) ⁶ (01020, 00122),	(10004) (01042, 00130),	(10011) (01023, 00102),		
(10011) (01020, 00132),	(10040) (01003, 00124),	(10040) (01022, 00102),	(10003) ³ (01033, 00102),	(10022) (01002, 00120),	(10030) (01020, 00133),	(10003) ⁶ (01031, 00111),	(10003) (01042, 00140),	(10022) (01024, 00132),		
(10022) (01023, 00142),	(10030) (01004, 00124),	(10030) (01011, 00113),	(10001) ³ (01041, 00102),	(10010) (01020, 00114),	(10044) (01034, 00143),	(10003) ³ (01040, 00104),	(10022) (01040, 00104),	(10030) (01040, 00104),		
(10012) ⁶ (01002, 00103),	(10014) (01030, 00100),	(10021) (01030, 00120),	(10034) (01000, 00133),	(10041) (01000, 00103),	(10043) (01033, 00100),	(10012) ⁶ (01001, 00114),	(10014) (01034, 00111),	(10021) (01041, 00110),		
(10034) (01004, 00144),	(10041) (01011, 00143),	(10043) (01044, 00140),	(10013) ⁶ (01000, 00111),	(10024) (01004, 00101),	(10023) (01010, 00100),	(10032) (01000, 00101),	(10031) (01011, 00100),	(10042) (01010, 00140),		
(10012) ⁶ (01001, 00132),	(10014) (01042, 00103),	(10021) (01023, 00110),	(10034) (01030, 00144),	(10041) (01030, 00124),	(10043) (01044, 00103),	(10012) ⁶ (01011, 00101),	(10014) (01010, 00141),	(10021) (01010, 00111),		
(10034) (01021, 00140),	(10043) (01004, 00112),	(10041) (01014, 00101),	(10013) ⁶ (01012, 00134),	(10023) (01012, 00134),	(10024) (01012, 00134),	(10031) (01043, 00121),	(10032) (01043, 00121),	(10042) (01043, 00121),		
(10014)<										

$(10131), (14044), (10143), (14030), (10104), (10412), (10111), (10400), (10123),$
 $(101031), (00142), (01040), (00104), (01140), (01041), (01111), (01000), (01132),$
 $(10443), (10130), (10431), (10142), (10424), (10102), (10230), (10114), (10204),$
 $(101014), (01103), (01023), (01124), (01032), (01210), (01342), (01243), (01332),$
 $(10121), (10223), (10133), (10242), (10140), (10211), (10100), (10301), (10112),$
 $(10221), (01322), (01204), (01312), (01232), (01302), (01320), (01441), (01310),$
 $(10332), (10124), (10313), (10131), (10344), (10143), (10320), (10104), (10111),$
 $(10443), (01300), (01440), (01340), (01442), (01330), (01444), (01430), (01432),$
 $(10123), (10130), (10142), (10204), (13022), (10211), (13013), (10223), (13004),$
 $(10434), (01431), (01433), (01013), (00123), (01040), (00104), (01022), (00130),$
 $(10230), (10242), (13031), (10202), (10300), (10214), (10343), (10221),$
 $(10004), (00111), (01031), (00142), (01101), (01001), (01114), (01033), (01122),$
 $(10331), (10233), (10324), (10240), (10312), (10201), (10431), (10213), (10400),$
 $(101010), (01130), (01042), (01143), (01024), (01224), (01311), (01213), (01331),$
 $(10220), (10232), (10244), (10443), (10244), (10412), (10203), (10210), (10222),$
 $(10202), (01301), (01241), (01321), (01230), (01341), (01413), (01414), (01410),$
 $(10234), (10241), (12002), (12043), (12034), (12020), (12011), (10304), (10311),$
 $(10411), (01412), (00144), (00113), (00132), (00101), (00120), (01100), (01142),$
 $(10323), (10330), (10342), (10301), (10313), (10320), (10332), (10344), (10302),$
 $(101134), (01121), (01113), (01222), (01233), (01244), (01200), (01211), (01340),$
 $(10434), (10314), (10410), (10321), (10441), (10333), (10422), (10340), (10403),$
 $(10442), (01320), (10441), (01300), (10440), (01330), (10444), (01310), (10443),$
 $(11040), (11031), (11022), (11013), (11004), (10403), (10410), (10422), (10434),$
 $(00100), (00143), (00131), (00124), (00112), (01134), (01113), (01142), (01121),$
 $(10441), (10401), (10413), (10420), (10432), (10444),$
 $(01100), (01211), (01233), (01200), (01222), (01244),$

$n_5(5, 2; 8) \geq 176: (01001), (14013), (01001), (14004), (01020), (14023), (01032),$
 $(00133), (00134), (00140), (00014), (00131), (00102), (00110),$
 $(14201), (01033), (14020), (01104), (14021), (01301), (14043), (10020), (10410),$
 $(00011), (00143), (00144), (00014), (00114), (00012), (00132), (00001), (01002),$
 $(10000), (10403), (10001), (10413), (10012), (10424), (10012), (10431), (10032),$
 $(00104), (01000), (00111), (01044), (00104), (01021), (00112), (01040), (00103),$
 $(10441), (10032), (10400), (10030), (10430), (10004), (10213), (10001), (10013),$
 $(01013), (00111), (01031), (00123), (01003), (01004), (01400), (01040), (01013),$
 $(10010), (10023), (10114), (10042), (10113), (10002), (10134), (10024), (10131),$
 $(01400), (10020), (00102), (01032), (01401), (01132), (01442), (01131), (01110),$
 $(10033), (10021), (10003), (10031), (10011), (10414), (10044), (10342), (10044),$
 $(01103), (10443), (10233), (01432), (01222), (01240), (01203), (01244), (01220),$
 $(13031), (10041), (10014), (10202), (10010), (10034), (10331), (10043), (10040),$
 $(00122), (01230), (01314), (01420), (01330), (01303), (01213), (01333), (01421),$
 $(10022), (10410), (10411), (10101), (10423), (10110), (10123), (13000),$
 $(10434), (01324), (01234), (10104), (01043), (01023), (01011), (01030), (00103),$
 $(10223), (10121), (10420), (10132), (12043), (10143), (10321), (10104), (10200),$
 $(01214), (01031), (01414), (01010), (00101), (01012), (01110), (01144), (01401),$
 $(10121), (10420), (10120), (10131), (10421), (10103), (10300), (10133), (10234),$
 $(01101), (01402), (01143), (10124), (01120), (01232), (01133), (01211), (01200),$
 $(10141), (10422), (10144), (13020), (10142), (10100), (10102), (10120), (10120),$
 $(01201), (01444), (01210), (00121), (01224), (01323), (01343), (01144), (01304),$
 $(10340), (10122), (12022), (10244), (10111), (10424), (10124), (10332), (10130),$
 $(01012), (01330), (00133), (01241), (01411), (01420), (01433), (01243), (01421),$
 $(10140), (10244), (10204), (10211), (10220), (10232), (10230), (10240), (10334),$
 $(10442), (01014), (01041), (01030), (01042), (01022), (01423), (101034), (101024),$
 $(10203), (10323), (10320), (10201), (10223), (01233), (10214), (10243), (13010), (10240),$
 $(01102), (01130), (10121), (10223), (01233), (01331), (01234), (01403), (10120), (01204),$
 $(10312), (10200), (10212), (10303), (10211), (10434), (10222), (10224), (10233),$
 $(10124), (01310), (01311), (01314), (01322), (01230), (01302), (01342), (01300),$
 $(11034), (10241), (10432), (12010), (11040), (10231), (10431), (10242), (10344),$
 $(00130), (01331), (10441), (00142), (00140), (01434), (01111), (01431), (01343),$
 $(10314), (10322), (10341), (10320), (10324), (10333), (11030), (10313), (10441),$
 $(10402), (10104), (01334), (01100), (01123), (01201), (00113), (01242), (01341),$
 $(10312), (12032), (10442), (10301), (10443), (10300), (10304), (10311), (10444),$
 $(01310), (00131), (01112), (01402), (01210), (01412), (01412), (01404), (01121),$
 $(10310), (10333), (10330), (11043), (10402), (10404), (10401), (10403), (13041),$
 $(10413), (01424), (01430), (00100), (01342), (01114), (01432), (01221), (00124),$
 $(13043), (11012), (10402), (12024), (13013), (13302), (11101),$
 $(00123), (00121), (01410), (00141), (00142), (00013), (00010),$

$n_5(5, 2; 11) \geq 260: (00102), (01104), (01002), (01003), (01030), (01012), (01044),$
 $(00012), (00013), (00014), (00012), (00013), (00014), (00012), (00013),$
 $(01021), (01200), (01300), (01440), (10001), (10002), (10001), (10002), (10004),$
 $(00110), (00011), (00010), (00001), (00012), (00013), (00014), (00012), (00013),$
 $(10002), (10003), (10004), (10004), (10103), (14043), (10101), (14012), (10110),$
 $(00014), (00013), (00014), (00012), (01004), (00111), (01024), (00113), (01013),$
 $(14034), (10113), (14003), (10122), (14020), (10120), (14044), (10132), (14030),$
 $(00123), (01033), (00120), (01022), (00130), (01042), (00132), (01001), (00144),$
 $(10134), (14011), (10144), (14021), (10141), (14002), (10104), (10444), (10102),$
 $(101031), (00142), (01010), (00101), (01040), (00104), (01103), (01023), (01113),$
 $(10410), (10111), (10432), (10114), (10403), (10121), (10441), (10123), (10420),$
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 (01231), (01203), (01204), (01204), (01221), (01221), (01233), (01242), (01242),
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 (01242), (01200), (01214), (01214), (01214), (01221), (01221), (01220), (01243),
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 (10243), (01210), (01210), (01222), (01231), (01231), (01231), (01243), (01243),
 (10444), (11000), (11004), (14001), (14001), (14001), (14001), (11203), (13402),
 (01242), (00014), (00014), (00014), (00014), (00014), (00014), (00010),

$(100vv), (101vv), (10000), (101vv), (010v1)^7, (100v1), (11000), (10000), (101v1), (100v1),$
 $(010vv), (010vv), (011vv), (01100), (001v1)^7, (00100), (001v1), (010v1), (01000), (011v1),$
 $(10100), (1\omega001)^7, (10\omega v0), (10v0v), (1001v), (1011v), (10\omega\omega\omega), (10\omega1\omega), (1\omega0\omega0)^7, (10\omega0v),$
 $(011v1), (0011v)^7, (0101v), (0111v), (01\omega\omega0), (01\omega11), (01\omega v1), (01v01), (00111), (01011),$
 $(10v10), (10011), (10111), (10\omega v\omega), (10\omega v1), (1\omega0v\omega)^7, (10\omega\omega0), (10v\omega1), (10011), (10111),$
 $(01111), (01\omega0\omega), (01\omega\omega1), (01\omega\omega v), (01v\omega0), (00111), (01011), (01111), (01\omega10), (01\omega0\omega),$
 $(10\omega0v), (10\omega\omega v), (1\omega0\omega v)^7, (10\omega10), (10v1\omega), (100v\omega), (101v\omega), (10\omega01), (10\omega11), (1\omega0\omega v)^7,$
 $(01\omega1\omega), (01vv\omega), (001v\omega), (010v\omega), (011v\omega), (01\omega v0), (01\omega0v), (01\omega vv), (01v\omega v), (001v\omega),$
 $(10\omega10), (10v1\omega), (100v\omega), (101v\omega), (10\omega01), (10\omega11), (1v001)^7, (10v01), (10\omega0\omega), (10v00),$
 $(10001), (10101), (10v01), (1v01v)^7, (10vvv), (10\omega\omega1), (10v10), (1000v), (1010v), (10v\omega v),$
 $(1v0v\omega)^7, (10v0\omega), (01v00), (0010v), (1000v), (1011v), (01\omega1v), (01v11), (01v1v), (01v\omega0),$
 $(0011\omega), (0101\omega), (0111\omega), (01\omega v\omega), (01v0v), (01v\omega v), (01v\omega0), (001\omega\omega), (010\omega\omega), (011\omega\omega),$
 $(10v\omega v), (100\omega\omega), (101\omega\omega), (10v1v), (1v01v)^7, (10v00), (10\omega\omega1), (10vv\omega), (100\omega1), (101\omega1),$
 $(01\omega01), (01v10), (01\omega\omega1), (01v1v), (001\omega1), (010\omega1), (011\omega1), (01\omega1v), (01v00), (01v1v),$
 $(10vv\omega),$
 $(01v1v)^7.$

$$n_4(5, 2; 9) \geq 141, \begin{bmatrix} 00100 \\ 10000 \\ 01100 \\ 00010 \\ 00001 \end{bmatrix} : (00010)^1, (010\omega v)^7, (1000\omega), (110\omega1), (100\omega1), (1010\omega),$$

$(100\omega v), (101\omega1), (010v1)^7, (10001), (110v0), (100v0), (10101), (100v1), (101v0), (010v1)^7,$
 $(0110\omega), (011\omega v), (00101), (001v0), (001v1), (010v0), (01101), (011v1), (011v1), (011v1), (011v1),$
 $(1000v), (110v\omega), (100v\omega), (1010v), (100v1), (101v\omega), (01000)^7, (1001v), (1101v), (1001v),$
 $(001v\omega), (001v1), (010v), (010v\omega), (011v), (011v1), (0011v), (0011v), (00100), (0010v),$
 $(0111v), (10000), (1011v), (010\omega v)^7, (10011), (110v\omega), (100v\omega), (10111), (100\omega v), (011v\omega),$
 $(0101v), (0111v), (01100), (00111), (001v\omega), (001\omega v), (01011), (010v\omega), (01111), (011\omega v),$
 $(010\omega\omega)^7, (100\omega1), (1100v), (1000v), (101\omega1), (100\omega\omega), (1010v), (1\omega00v)^7, (10\omega00), (10v0\omega),$
 $(001\omega1), (0010v), (001\omega\omega), (010\omega1), (0100v), (011\omega1), (011\omega\omega), (0010\omega), (0100\omega), (0110\omega),$
 $(1000\omega), (1010\omega), (10\omega01), (10\omega01), (1\omega0v0)^7, (10\omega\omega1), (10v\omega0), (1001\omega), (0111\omega), (10\omega0v),$
 $(01\omega00), (01\omega0v), (01\omega0v), (01v0v), (0011\omega), (0101\omega), (0111\omega), (01\omega1v), (01\omega0\omega), (01\omega11),$
 $(10\omega\omega\omega), (1\omega00\omega)^7, (10\omega1v), (10v01), (100\omega0), (101\omega0), (10\omega v1), (10\omega\omega\omega), (1\omega0\omega0)^7, (10\omega\omega1),$
 $(01vv0), (001\omega0), (010\omega0), (011\omega0), (01\omega v\omega), (01\omega11), (01v0\omega), (01v0\omega), (01\omega\omega\omega), (010\omega\omega),$
 $(10v10), (100\omega\omega), (101\omega\omega), (10\omega\omega1), (10\omega0\omega), (1\omega00\omega)^7, (10\omega\omega v), (10v01), (100v0), (01v01),$
 $(011\omega\omega), (011v\omega), (01\omega1\omega), (01\omega01), (01v00), (001v0), (010v0), (011v0), (01\omega1\omega), (01\omega v\omega),$
 $(10\omega11), (10\omega v\omega), (1\omega0\omega v)^7, (10\omega1v), (10v1\omega), (100vv), (101vv), (10\omega0v), (10\omega10), (1v010)^7,$
 $(01\omega\omega1), (01v0\omega), (001vv), (010vv), (011vv), (01\omega v\omega), (01\omega0\omega), (01\omega v0), (01v\omega v), (01000),$
 $(10vv0), (10\omega\omega0), (10v10), (10000), (10100), (10v\omega0), (1v0\omega0)^7, (10v1\omega), (10\omega v0), (10\omega\omega1),$
 $(10000), (01100), (01\omega10), (01vv0), (01vv0), (00101), (01001), (01001), (01101), (01\omega00),$
 $(10001), (10101), (10vvv), (1v000)^7, (10vv\omega), (10\omega00), (10v11), (10011), (01111), (10vvv),$
 $(01vv\omega), (01v11), (01vv\omega), (00111), (01011), (01111), (01\omega00), (01vvv), (01v11), (01v\omega\omega),$
 $(1v0\omega\omega)^7, (10vv1), (10vvv), (10vv\omega), (10010), (10110), (10v0v), (1v0\omega\omega)^7, (10vv1), (10vvv),$
 $(00110), (01010), (01110), (01\omega\omega\omega), (01v1\omega), (01v01), (01v1v), (00110), (01010), (01110),$
 $(10vv\omega), (10010), (10110), (10v0v), (1v0v1)^7, (10v00), (10\omega1\omega), (10vv\omega), (1001\omega), (011\omega),$
 $(01\omega\omega\omega), (01v1\omega), (01v01), (01v1v), (0011\omega), (101\omega), (01\omega1\omega), (01\omega v1), (01v00), (01v1v),$
 $(10vv\omega), (1v0v1)^7, (10v1v), (10\omega1\omega), (10v11), (100\omega0), (101\omega0), (10v0\omega), (1v0v\omega)^7, (10v0v),$
 $(01vv1), (001\omega0), (010\omega0), (011\omega0), (01\omega v1), (01v\omega1), (01v0v), (01v\omega\omega), (001vv), (010vv),$
 $(10\omega v1), (10v10), (100vv), (101vv), (10v1v),$
 $(011vv), (01\omega v\omega), (01v01), (01v\omega1), (01v\omega v).$

$$n_4(5, 2; 10) \geq 156, \begin{bmatrix} 0\omega000 \\ \omega0000 \\ 000v0 \\ 00v00 \\ 00001 \end{bmatrix}, x \rightarrow x^2: (001\omega0)^2, (001v0), (01000)^2, (10000), (01000)^2,$$

$(10000), (0101\omega)^{12}, (0101v), (010\omega1), (010\omega\omega), (010v1), (010vv), (1010\omega), (1010v), (10\omega01),$
 $(00100), (00101)^{12}, (00101), (0010\omega), (0010\omega), (0010v), (0010v), (00011), (00011), (0001\omega),$
 $(10\omega0\omega), (10v01), (10v0v), (1\omega01v)^6, (1\omega0\omega\omega), (1\omega0v1), (1v01\omega), (1v0\omega1), (1v0vv), (1\omega01\omega)^6,$
 $(0001\omega), (0001v), (0001v), (0011\omega), (0011v), (00111), (0011v), (00111), (0011\omega), (001\omega\omega)^6,$
 $(1\omega0\omega1), (1\omega0vv), (1v01v), (1v0\omega\omega), (1v0v1), (100\omega0)^{12}, (100v0), (10010), (100v0), (10010),$
 $(001\omega v), (001\omega1), (001vv), (001v1), (001v\omega), (0101\omega)^{12}, (0101v), (010\omega\omega), (010\omega1), (010vv),$
 $(100\omega0), (10\omega0\omega), (10v0v), (1010\omega), (10v01), (1010v), (10\omega01), (101\omega0)^{12}, (101v0), (10\omega10),$
 $(010v1), (01100), (01100), (01\omega00), (01\omega00), (01v00), (01v00), (01001)^{12}, (01001), (0100v),$
 $(10\omega v0), (10v10), (10v\omega0), (1000v), (1000\omega), (10001), (1000\omega), (10001), (1000v), (10111)^6,$
 $(0100v), (0100\omega), (0100\omega), (011\omega0), (011v0), (01\omega10), (01\omega v0), (01v10), (01v\omega0), (01011)^6,$
 $(10\omega v\omega), (10vv\omega), (10101), (10\omega0v), (10v0\omega), (10111)^6, (10\omega\omega v), (10vv\omega), (10101), (10\omega0v),$
 $(010\omega v), (010v\omega), (01111), (01\omega v\omega), (01v\omega\omega), (01011), (010\omega v), (010v\omega), (01111), (01\omega\omega v),$
 $(10v0\omega), (101\omega0)^{12}, (101v0), (10\omega10), (10\omega v0), (10v10), (10v\omega0), (1010\omega), (1010v), (10\omega0\omega),$
 $(01vv\omega), (010\omega\omega)^{12}, (010vv), (0101\omega), (010v1), (0101v), (010\omega1), (011\omega0), (011v0), (01\omega10),$
 $(10\omega01), (10v0v), (10v01), (1001v)^6, (1001\omega), (100\omega\omega), (100\omega1), (100vv), (100v1), (100\omega\omega)^6,$
 $(01\omega v0), (01v10), (01v\omega0), (0110\omega), (0110v), (01\omega01), (01\omega0\omega), (01v01), (01v0v), (0110\omega)^6,$
 $(100vv), (1001\omega), (100v1), (1001v), (100\omega1), (1001v)^{12}, (1001\omega), (10\omega1\omega), (10v1v), (100\omega1),$
 $(0110v), (01\omega0\omega), (01\omega01), (01v0v), (01v01), (011\omega\omega), (011vv), (0110v), (0110\omega), (01\omega1\omega),$
 $(100\omega\omega), (101\omega\omega), (10vv1), (100v1), (100vv), (101vv), (10\omega v1), (100v\omega)^{12}, (100\omega v), (10\omega v\omega),$
 $(01\omega v1), (01\omega01), (01\omega0\omega), (01v1v), (01v\omega1), (01v01), (01v0v), (011\omega1), (011v1), (01101),$
 $(10vv\omega), (100v\omega), (10011), (101v\omega), (10v11), (10vv\omega), (101v1), (10\omega v\omega), (10v0\omega), (01\omega v\omega)^6,$
 $(01101), (01\omega1v), (01\omega vv), (01\omega0v), (01\omega0v), (01v1\omega), (01v\omega v), (011\omega v), (01v0\omega), (01\omega1\omega)^6,$
 $(101v\omega), (10\omega11), (10\omega\omega\omega), (10v11), (10vv\omega), (101v1)^{12}, (101\omega1), (10\omega vv), (10v\omega\omega), (101v1),$
 $(011v1), (01\omega1v), (01\omega vv), (01v1\omega), (01v\omega\omega), (011\omega v), (011v\omega), (011v\omega), (011\omega v), (01\omega\omega\omega)^6,$
 $(10vv\omega), (10\omega1v), (10v1v), (10v1\omega), (10v1\omega), (10v1\omega), (10v1\omega), (10v1\omega), (10v1\omega), (10v1\omega),$
 $(01\omega11), (01\omega v\omega), (01\omega11), (01vv\omega), (01v11), (01v11), (01v11), (01v\omega v), (01110)^{12}, (011v1), (01110),$
 $(10vv0), (101vv), (10110), (10vv0), (10v1v), (10110), (101\omega\omega), (10\omega\omega0), (10v1\omega), (10\omega\omega1),$
 $(011\omega\omega), (01\omega\omega0), (01\omega v1), (01\omega1\omega), (01\omega\omega0), (01v\omega1), (01v\omega0), (01v1v), (01v\omega0), (0111\omega)^6,$
 $(10\omega\omega1), (10\omega v\omega), (10vv1), (101v\omega), (1011v), (10vv\omega), (1011\omega), (101\omega\omega), (10\omega\omega\omega)^{12},$
 $(011v1), (0111v), (011\omega1), (01\omega\omega\omega), (01\omega vv), (01\omega1v), (01\omega\omega1), (01v\omega\omega), (01vv\omega), (01v1\omega),$
 $(10\omega11),$
 $(01vv1).$

$$\begin{aligned}
n_4(5, 2; 11) &\geq 175, \begin{bmatrix} 00100 \\ 10000 \\ 01100 \\ 00010 \\ 00001 \end{bmatrix} : (0101\omega)^7, (10001), (1101v), (1001v), (10101), (1001\omega), \\
&(1011v), (010\omega 0)^7, (1000\omega), (110\omega\omega), (100\omega\omega), (1010\omega), (100\omega 0), (101\omega\omega), (010\omega v)^7, (1000v), \\
&(110\omega 0), (100\omega 0), (1010v), (100\omega v), (101\omega 0), (010v 0)^7, (1000\omega), (110v\omega), (100v\omega), (1010\omega), \\
&(001\omega v), (0100v), (010\omega 0), (0110v), (011\omega v), (0010\omega), (001v\omega), (001v 0), (0100\omega), (010v\omega), \\
&(100v 0), (101v\omega), (01001)^7, (10010), (11011), (10011), (01110), (10001), (10111), (01010)^7, \\
&(0110\omega), (011v 0), (00110), (00111), (00101), (01010), (01011), (01110), (01101), (01101), \\
&(10011), (11001), (10001), (10111), (10010), (10101), (010\omega\omega)^7, (1001\omega), (110v 0), (100v 0), \\
&(00101), (00110), (01011), (01001), (01111), (01110), (0011\omega), (001v 0), (001\omega\omega), (0101\omega), \\
&(1011\omega), (100\omega\omega), (101v 0), (010v 1)^7, (1001\omega), (110\omega v), (100\omega v), (1011\omega), (100v 1), (101\omega v), \\
&(010v 0), (0111\omega), (011\omega\omega), (0011\omega), (001\omega v), (001v 1), (0101\omega), (010\omega v), (0111\omega), (011v 1), \\
&(0100v)^7, (100\omega v), (110\omega 0), (100\omega 0), (101\omega v), (1000v), (101\omega 0), (0100v)^7, (100v 1), (110v\omega), \\
&(001\omega v), (001\omega 0), (0010v), (010\omega v), (010\omega 0), (011\omega v), (0110v), (001v 1), (001v\omega), (0010v), \\
&(100v\omega), (101v 1), (1000v), (101v\omega), (0101v)^7, (100v\omega), (110\omega 1), (100\omega 1), (101v\omega), (1001v), \\
&(010v 1), (010v\omega), (011v 1), (0110v), (001v\omega), (001\omega 1), (0011v), (010v\omega), (010\omega 1), (011v\omega), \\
&(101\omega 1), (1\omega 0\omega)^7, (1\omega 0v), (1\omega 01), (10000), (10100), (1\omega 01), (1\omega 0\omega), (1\omega 0v)^7, (1\omega 11), \\
&(0111v), (00100), (01000), (01100), (01\omega 0v), (01\omega 01), (01v 0\omega), (01v 0\omega), (01000), (01000), \\
&(10v\omega\omega), (10000), (01000), (10\omega\omega\omega), (10\omega v\omega), (1\omega 01v)^7, (10\omega 11), (10v\omega\omega), (10010), (10110), \\
&(01100), (01\omega v\omega), (01\omega 11), (01\omega\omega\omega), (01v\omega v), (01110), (01010), (01110), (01\omega v\omega), (01\omega v\omega), \\
&(10\omega 1\omega), (10\omega 0v), (1\omega 0\omega\omega)^7, (1\omega 01), (10v 11), (1001v), (1011v), (10\omega v 0), (10\omega v 1), (1\omega 0v 0)^7, \\
&(01\omega 0\omega), (01v 1v), (0011v), (0101v), (0101v), (01\omega 0v), (01\omega 0\omega), (01\omega\omega v), (01v\omega\omega), (00111), \\
&(10\omega v\omega), (10v\omega 0), (10011), (10111), (10\omega 0\omega), (10\omega\omega 1), (1\omega 00v)^7, (10\omega 10), (10v\omega\omega), (100\omega\omega), \\
&(01011), (01111), (01\omega 1\omega), (01\omega 1v), (01\omega 01), (01\omega 1v), (001\omega\omega), (010\omega\omega), (010\omega\omega), (01\omega v 0), \\
&(101\omega\omega), (10\omega v 1), (10\omega\omega 1), (1\omega 001)^7, (10\omega\omega 0), (10v 0v), (100v\omega), (101v\omega), (10\omega 1\omega), (10\omega v\omega), \\
&(01\omega v\omega), (01\omega 1v), (01v 0v), (001v\omega), (010v\omega), (011v\omega), (01\omega 10), (01\omega v 1), (01\omega\omega 1), (01v 01), \\
&(1\omega 001)^7, (10\omega\omega 0), (10v 0v), (100v\omega), (101v\omega), (10\omega 1\omega), (10\omega v\omega), (1\omega 00v)^7, (10\omega v\omega), (10v 0\omega), \\
&(001v\omega), (010v\omega), (011v\omega), (01\omega 10), (01\omega v 1), (01\omega\omega 1), (01v 01), (001v\omega), (010v\omega), (011v\omega), \\
&(100v\omega), (101v\omega), (10\omega 1v), (10\omega v 0), (1\omega 0\omega 0)^7, (10\omega 10), (10v 10), (100v 0), (101v 0), (10\omega 00), \\
&(01\omega 1\omega), (01\omega v\omega), (01\omega\omega 0), (01v 0v), (001v 0), (010v 0), (011v 0), (01\omega v 0), (01\omega v 0), (01\omega v 0), \\
&(10\omega 10), (1\omega 0v\omega)^7, (10\omega v 0), (10v\omega 1), (100v 1), (101v 1), (10\omega v\omega), (10\omega 0v), (1v 01v)^7, (10v 1v), \\
&(01v 00), (001v 1), (010v 1), (011v 1), (01\omega\omega 0), (01\omega\omega\omega), (01\omega\omega\omega), (01v\omega\omega), (0010\omega), (0100\omega), \\
&(10\omega\omega 1), (10v 11), (1000\omega), (1010\omega), (10v\omega 0), (1\omega 00v)^7, (10v\omega 0), (10\omega 01), (10v\omega\omega), (100\omega 1), \\
&(0110\omega), (011v\omega), (01v 1\omega), (01v\omega\omega), (01v\omega 0), (001\omega 1), (010\omega 1), (011\omega 1), (01\omega 0v), (01v 10), \\
&(101\omega 1), (01v 1\omega), (1v 011)^7, (1\omega 01), (10\omega\omega\omega), (10v\omega 0), (100\omega 1), (101\omega 1), (10v 1v), \\
&(01v\omega\omega), (01v\omega\omega), (001\omega 1), (010\omega 1), (01\omega 11), (01v\omega\omega), (01v 1\omega), (01v\omega\omega). \\
\\
n_4(5, 2; 14) &\geq 222, \begin{bmatrix} 0\omega 000 \\ \omega 0000 \\ 000v 0 \\ 00v 00 \\ 00001 \end{bmatrix}, \begin{bmatrix} 00100 \\ 00010 \\ 10000 \\ 01000 \\ 00001 \end{bmatrix}, x \rightarrow x^2: (00010)^4, (00100), (01000), (10000), \\
&(01000)^2, (10000), (01001)^6, (0001\omega), (0100\omega), (0001v), (1000v), (1000\omega), (01001)^{12}, (0100v), \\
&(00010), (10001), (1000v), (1000\omega), (1001), (1100v), (11001), (1100v), (1100\omega), (1100v), \\
&(0011v), (00111), (0011\omega), (0011v), (00011), (0001\omega), (0001v), (00101), (0010\omega), (0010v), \\
&(11001)^6, (1100\omega), (1100v), (11000), (11000), (11000), (1\omega 000)^2, (1v 000), (1\omega 000)^2, (001v 0), \\
&(00110), (00110), (00110), (00111), (0011\omega), (0011v), (001\omega 0), (001v 0), (001\omega 0), (001v 0), \\
&(1\omega 000)^2, (1v 000), (1\omega 00\omega)^6, (1\omega 001), (1\omega 00v), (1v 00v), (1v 00\omega), (1v 001), (1\omega 010)^{24}, (1\omega 011), \\
&(001\omega 0), (001v 0), (001\omega 1), (001\omega\omega), (001v\omega), (001v\omega), (001v\omega), (001v\omega), (001\omega\omega), (001\omega\omega), \\
&(1\omega 0\omega), (1\omega 0v\omega), (1\omega 0v 0), (1\omega 0v 1), (1v 010), (1v 011), (1v 0\omega 0), (1v 0\omega v), (1v 0v 0), (1v 0v 0), \\
&(001\omega v), (001\omega v), (001\omega 1), (001\omega 1), (001v\omega), (001v\omega), (001v 1), (001v 1), (001v\omega), (001v\omega), \\
&(10\omega v\omega), (10\omega v 0), (10\omega v 1), (10\omega v 1), (101v 0), (101v 1), (101v 1), (101v 1), (101v 1), (101v 1), \\
&(011\omega 0), (011\omega 1), (011v 0), (011v 1), (01\omega 10), (01\omega 1v), (01\omega v 0), (01\omega v\omega), (01v 10), (01v 1\omega), \\
&(10\omega 11), (10\omega 10), (1010\omega)^{12}, (10100), (10100), (10100), (1010v), (1010\omega), (1010\omega), (10\omega 00), (10\omega 00), \\
&(01v\omega 0), (01v\omega\omega), (01010), (01010), (0101\omega), (0101v), (010\omega 0), (010\omega 0), (010\omega 1), (010\omega\omega), \\
&(10v 01), (10v 0v), (10v 00), (10v 00), (1010v)^{12}, (1010\omega), (1010v), (1010v), (1010v), (1010v), \\
&(010v 0), (010v 0), (010v 1), (010v\omega), (010\omega 1), (010\omega\omega), (01100), (100\omega 0), (100v 0), (10010)^3, \\
&(10\omega 01), (10\omega 0\omega), (10v 01), (10v 0v), (10v 01), (10v 0v), (10v 0v), (10010)^3, (10010)^3, (10011), \\
&(010v 1), (010v\omega), (0101\omega), (0101v), (010\omega 1), (010\omega\omega), (01100), (01\omega 00), (01v 00), (01100), \\
&(100\omega 0), (100v 0), (1001v)^6, (1001\omega), (100\omega\omega), (100\omega 1), (100v\omega), (100v 1), (10011)^{24}, (10011), \\
&(01\omega 00), (01v 00), (0110\omega), (0110v), (01\omega 01), (01\omega 0\omega), (01v 01), (01v 0v), (011\omega 0), (011\omega\omega), \\
&(10011), (10011), (10\omega 10), (10\omega 1\omega), (10v 10), (10v 1v), (100\omega v), (100\omega v), (100\omega v), (100\omega v), \\
&(011v 0), (011v\omega), (01101), (01101), (01101), (01101), (01\omega 10), (01\omega 1\omega), (01\omega v 0), (01\omega v 1), \\
&(101\omega 0), (101\omega\omega), (10v\omega 0), (10v\omega 1), (100v\omega), (100v\omega), (100v\omega), (100v\omega), (101v 0), (101v\omega), \\
&(01\omega 0v), (01\omega 0v), (01\omega 0v), (01\omega 0v), (01v 10), (01v 1v), (01v\omega 0), (01v\omega 1), (01v\omega 0), (01v\omega 0), \\
&(10\omega v 0), (10\omega v 1), (1001v)^{24}, (1001v), (1001\omega), (1001\omega), (10\omega 1\omega), (10\omega 1v), (10v 1\omega), (10v 1v), \\
&(01v\omega\omega), (01v\omega\omega), (011\omega\omega), (011v\omega), (011v\omega), (011v\omega), (0110v), (0110v), (0110\omega), (0110\omega), \\
&(100\omega 1), (100\omega 1), (100\omega\omega), (100\omega\omega), (101\omega 1), (101\omega\omega), (10v\omega 1), (10v\omega\omega), (10v 11), (10v 1v), \\
&(01\omega 11), (01\omega 1\omega), (01\omega v 1), (01\omega v\omega), (01\omega 01), (01\omega 01), (01\omega 0\omega), (01\omega 0\omega), (01v 11), (01v 1v), \\
&(100v\omega), (100v\omega), (101v 1), (101v\omega), (10\omega v 1), (10\omega v\omega), (101\omega 0)^{24}, (101\omega 1), (101v 0), (101v 1), \\
&(01v\omega 1), (01v\omega\omega), (01v 01), (01v 01), (01v 0v), (01v 0v), (01111), (0111v), (01111), (0111\omega), \\
&(10\omega v\omega), (10\omega\omega 1), (10v\omega\omega), (10v\omega 1), (10111), (1011v), (10\omega 1v), (10\omega\omega\omega), (10\omega v\omega), (10\omega v\omega), \\
&(011\omega 0), (011\omega\omega), (011v 0), (011v\omega), (01\omega 10), (01\omega 11), (01\omega\omega 1), (01\omega\omega\omega), (01\omega\omega\omega), (01\omega\omega\omega), \\
&(10v\omega\omega), (10v\omega\omega), (10111), (1011\omega), (10\omega\omega\omega), (10\omega\omega\omega), (10v 1\omega), (10v 10), (10v\omega 0), (10v\omega\omega), \\
&(01\omega v 0), (01\omega v\omega), (01v 10), (01v 11), (01v\omega 0), (01v\omega\omega), (01v 1v), (01v\omega\omega), (01v\omega\omega), (01v\omega\omega), \\
&(1011\omega)^{24}, (10110), (10110), (1011v), (1011v), (10\omega 1v), (10\omega 1\omega), (10v 1v), (10v 1v), (101\omega 1), (101\omega\omega), \\
&(011\omega\omega), (011\omega\omega), (011v\omega), (011v\omega), (011v\omega), (01110), (0111\omega), (01110), (0111v), (01\omega\omega 0), (01\omega\omega\omega), \\
&(10\omega\omega 0), (10\omega\omega\omega), (10\omega\omega 1), (10\omega\omega\omega), (10\omega\omega 0), (10\omega\omega 1), (101v 1), (101v\omega), (10v\omega v), (10v\omega v), \\
&(01\omega 11), (01\omega 1\omega), (01\omega v 1), (01\omega v\omega), (01\omega\omega 0), (01\omega\omega 1), (01v\omega 0), (01v\omega\omega), (01v\omega 0), (01v\omega 0), \\
&(10v\omega 0), (10v\omega\omega), (10v 1v), (10v\omega 0), (10v\omega 0), (101\omega\omega)^{24}, (101\omega\omega), (10\omega\omega\omega), (10\omega\omega\omega), (10v\omega 0), \\
&(01v 11), (01v 1v), (01v\omega 1), (01v\omega\omega), (011\omega 1), (011v 1), (0111v), (011v 0), (011v 1), (011\omega 0), \\
&(10v\omega v), (10v\omega\omega), (10v 1v), (10v\omega 0), (10v\omega\omega), (10v 11), (10v 11), (10v 11), (10v 10), (10v 10), \\
&(011\omega 1), (011\omega 0), (01\omega\omega 1), (01\omega v 0), (01\omega v\omega), (01\omega 1v), (01\omega v\omega), (01\omega 1v), (01\omega 10), (01\omega\omega\omega), \\
&(1011v), (101\omega\omega), (101\omega 0), (10\omega 11), (10\omega 10), (10v\omega v), (10v\omega\omega), (10v\omega\omega), (10v\omega\omega).
\end{aligned}$$

$$n_4(5, 2; 18) \geq 290, \begin{bmatrix} 0\omega 000 \\ \omega 0000 \\ 000v0 \\ 00v00 \\ 00001 \end{bmatrix}, \begin{bmatrix} 00100 \\ 00010 \\ 10000 \\ 01000 \\ 00001 \end{bmatrix} : (001\omega 0)^4, (001v0), (1\omega 000), (1v000), (00101)^{12},$$

(0010 ω), (0010 v), (00100), (00100), (00100), (10001), (1000 ω), (1000 v), (10000), (01001), (01000),
(00010), (00010), (00011), (0001 ω), (0001 v), (01000), (01000), (01000), (0101 ω)¹², (010 ω 1), (010 v 1),
(1010 ω), (10 ω 01), (10 v 0 v), (1000 ω), (10001), (1000 v), (1010 ω), (10 ω 01), (10 v 0 v), (0101 ω)¹²,
(0001 ω), (0001 v), (00011), (0101 ω), (010 ω 1), (010 v 1), (0100 ω), (01001), (0100 v), (0100 ω),
(010 ω 1), (010 v 1), (010 ω), (10 ω 01), (10 v 0 v), (1000 ω), (10001), (1000 v), (1010 ω), (10 ω 01),
(0010 v), (00101), (0001 ω), (0001 v), (00011), (0101 ω), (010 ω 1), (010 v 1), (0100 ω), (01001),
(10 v 0 v), (01000)⁴, (10000), (11000), (11000), (1 ω 011)¹², (1 ω 0 ω 1), (1 ω 0 v 1), (1 v 01 v), (1 v 0 ω 1),
(0100 v), (00110), (00110), (00010), (00100), (0011 v), (00111), (0011 ω), (00111), (0011 ω),
(1 v 0 v 1), (101 ω 1), (101 v 1), (10 ω 11), (10 ω 11), (10 v 1 v), (10 v 1 v), (1 ω 01 ω)¹², (1 ω 0 ω 1), (1 ω 0 v 1),
(0011 v), (011 ω 1), (011 v 1), (01 ω 1 ω), (01 ω 1 v), (01 v 1 ω), (01 v 1 v), (001 ω 1), (001 ω 1), (001 ω 1),
(1 v 010), (1 v 0 ω 0), (1 v 0 v 0), (10 ω 1 ω), (10 v 1 v), (10 v 1 v), (10 v 10), (10 ω 1 ω), (10 ω 1 ω), (1 ω 000)²,
(001 v 1), (001 v 1), (001 v 1), (011 ω 1), (011 v 1), (01 ω 10), (01 ω 1 v), (01 v 1 v), (01 v 1 v), (01 v 1 v),
(1 v 000), (1 ω 000)², (1 v 000), (1 ω 000)², (1 v 000), (1010 v)⁶, (10101), (10 ω 0 v), (10 ω 0 ω), (10 v 0 v),
(001 ω 0), (001 v 0), (001 ω 0), (001 v 0), (001 ω 0), (01011), (0101 v), (010 ω 1), (010 v 1), (010 v 1),
(10 v 01), (1010 v)⁶, (1010 ω), (10 ω 0 ω), (10 ω 01), (10 v 0 v), (10 v 01), (101 ω)¹², (101 ω 1), (10 ω 1),
(010 v 1), (0101 ω), (0101 v), (010 ω 1), (010 ω 1), (010 v 1), (010 v 1), (0101 v), (0101 v), (010 ω)¹²,
(10 ω 1 ω), (10 v 11), (10 v 1 v), (10 v 01), (10 v 01), (1010 v), (1010 v), (10 ω 0 ω), (10 ω 0 ω), (101 v)¹²,
(010 ω 1), (010 v 1), (0101 v), (011 v 1), (011 v 1), (01 ω 1 v), (01 ω 1 v), (01 ω 1 v), (01 ω 1 v), (01 ω 1 v),
(101 v 1), (10 ω 11), (10 ω 1 v), (10 v 1 v), (10 v 1 v), (10 ω 0 v), (10 ω 0 v), (10 ω 0 v), (10 ω 0 v), (10101),
(01011), (010 ω 1), (010 v 1), (010 ω 1), (010 v 1), (011 ω 1), (011 ω 1), (01 ω 1 v), (01 ω 1 v), (01 ω 1 v),
(10101), (1011 v)¹², (101 v 1), (10 ω 1 ω), (10 ω 1 ω), (10 v 1 v), (10 v 1 v), (10100), (10 ω 00), (10 ω 00),
(01 v 1 ω), (010 ω 0), (010 v 0), (01010), (010 ω 0), (01010), (010 ω 0), (010 ω 0), (010 ω 0), (010 ω 0),
(10 v 00), (10100), (10 v 00), (1011 v)¹², (101 v 1), (10 ω 1 ω), (10 ω 1 ω), (10 v 1 v), (10 v 1 v), (10101),
(01 ω 1 ω), (01 v 1 v), (01 v 1 v), (010 ω 1), (010 ω 1), (010 v 1), (010 v 1), (010 v 1), (010 v 1), (010 v 1),
(10 ω 0 v), (10 ω 0 v), (10 v 0 ω), (10101), (10 v 0 ω), (101 ω)¹², (10111), (10 ω 1 ω), (10 ω 1 ω), (10 v 1 ω),
(0111 v), (01 ω 1 ω), (01 ω 1 ω), (01 v 1 v), (01 v 1 v), (01 v 1 v), (01 v 1 v), (01 v 1 v), (01 v 1 v), (01 v 1 v),
(10 v 1 ω), (10100), (10 v 00), (10100), (10 ω 00), (10 ω 00), (10 v 00), (10 v 00), (10011)⁶, (10010), (100 ω 1),
(010 ω 0), (011 v 1), (011 v 1), (011 v 1), (011 v 1), (01 ω 1 ω), (01 ω 1 ω), (01 ω 1 ω), (01100), (01101), (01 ω 00),
(100 ω 0), (100 v 1), (100 v 0), (1001 ω)⁶, (10010), (100 ω 1), (100 ω 0), (100 v 1), (100 v 0), (1001 v)³,
(01 ω 0 ω), (01 v 0 ω), (01 v 0 ω), (01100), (01100), (0110 ω), (01 ω 00), (01 v 00), (01 v 00), (01 v 00),
(100 ω 1), (100 v 1), (1001 v)³, (100 ω 1), (100 v 1), (100 v 1), (100 v 1), (100 v 1), (100 v 1), (100 v 1),
(01 ω 0 ω), (01 v 01), (0110 v), (010 ω 1), (010 ω 1), (0101 v), (0101 v), (0101 v), (0101 v), (0101 v),
(100 v 1), (10 ω 1 v), (10 v 1 v), (101 v 1), (100 ω 1), (10111), (10 v 1 ω), (10010)⁶, (10 ω 11), (100 ω 0),
(01 ω 1 ω), (01 ω 0 ω), (01 ω 0 ω), (01 ω 11), (01 v 1 v), (01 v 1 v), (01 v 1 v), (01 v 1 v), (01 v 1 v), (01 v 1 v),
(10 v 1 ω), (100 v 0), (101 v 1), (100 v 1)¹², (100 ω 1), (10 ω 1 ω), (10 v 1 ω), (10 v 1 ω), (100 v 1), (101 v),
(01 ω 00), (01 v 1 ω), (01 v 00), (011 ω 0), (011 v 0), (011 v 0), (011 ω 0), (011 ω 0), (011 ω 0), (011 ω 0),
(10 v 1 ω), (100 ω 1), (1001 ω), (101 ω 1), (10 ω 10), (10011)¹², (10011), (10 v 10), (10 v 1 v), (100 v 1),
(01 ω 01), (01 v 10), (01 v 0 v), (01 v 0 v), (01 v 0 v), (011 v 0), (011 v 0), (01101), (01101), (01 ω 10),
(100 v 1), (101 ω 0), (101 ω 1), (100 v 1), (100 v 1), (10 ω 1 ω), (10 ω 1 ω), (10011)¹², (10011), (10 v 10),
(01 ω 1 ω), (01 ω 0 v), (01 ω 0 v), (01 v 0 v), (01 v 0 v), (01 v 0 ω), (01 v 0 ω), (011 v 0), (011 v 0), (01101),
(10 v 1 v), (100 v 1), (100 v 1), (101 ω 0), (101 ω 0), (100 v 1), (100 v 1), (100 v 1), (10 ω 1 ω), (101 ω)¹²,
(01101), (01 ω 10), (01 ω 10), (01 ω 0 v), (01 ω 0 v), (01 v 0 v), (01 v 0 v), (01 v 0 v), (01 v 0 v), (011 ω)¹²,
(101 ω 0), (10 v 1 v), (10 v 1 v), (0111 v), (0111 v), (10 ω 1 ω), (10 ω 1 ω), (10 ω 10), (10 v 1 ω), (10111),
(0111 v), (0111 v), (0111 v), (0111 v), (0111 v), (0111 v), (0111 v), (0111 v), (0111 v), (0111 v),
(1011 ω), (10 ω 00), (10 ω 1 ω), (10111)¹², (10110), (10 ω 1 ω), (10 ω 11), (10 ω 00), (10 ω 1 ω), (10 ω 1 ω),
(0111 v), (01 v 1 ω), (01 v 1 ω), (011 ω 1), (011 ω 1), (011 ω 1), (0111 v), (0111 v), (0111 v), (0111 v),
(10 ω 1 ω), (101 v 1), (101 v 1), (10 v 1 ω), (10 v 1 ω), (101 v 0), (101 v 0), (101 v 0), (101 v 0), (101 v 0),
(01 ω 1 ω), (01 v 0 v), (01 v 0 v), (01 v 0 v), (01 v 0 v), (011 v 1), (011 v 1), (011 v 1), (011 v 1), (011 v 1),
(10 ω 10), (10 v 1 v), (10 ω 11), (0111 v), (0111 v), (10 ω 1 ω), (10 ω 1 ω), (10 ω 00), (1011 ω)⁶, (10 v 1 v), (101 ω 1),
(01 ω 1 ω), (01 v 1 ω), (01 v 1 ω), (01 v 1 ω), (01 v 1 ω), (01 v 10), (01 v 11), (0111 v), (0111 v), (0111 v),
(10 ω 1 ω), (10 ω 1 ω), (10 v 1 v), (101 ω)¹², (10 ω 1 ω), (10 v 1 v), (10 v 1 v), (101 v 0), (101 v 0), (101 v 0),
(01 ω 1 ω), (01 v 1 v), (01 v 1 v), (0111 v), (0111 v), (0111 v), (0111 v), (0111 v), (0111 v), (0111 v),
(10 v 11), (101 ω 1), (10 ω 11), (10 ω 10), (10 v 11), (01 v 1 ω), (01 v 1 ω), (01 v 1 ω), (01 v 1 ω), (01 v 1 ω),
(01 ω 1 ω), (01 v 1 v), (01 v 1 v), (01 v 10), (01 v 10), (0111 v), (0111 v), (01 ω 1 ω), (01 ω 1 ω), (01 ω 1 ω),

$$n_4(5, 2; 19) \geq 307, \begin{bmatrix} 0\omega 000 \\ \omega 0000 \\ 000v0 \\ 00v00 \\ 00001 \end{bmatrix}, x \rightarrow x^2: (00100)^1, (00100)^1, (00100)^1, (01000)^2, (10000),$$

(01000)⁶, (01000), (01000), (00010), (10000), (10000), (0100 ω)¹², (0100 v), (01001), (0100 ω), (0100 ω),
(01001), (0100 v), (1000 ω), (1000 v), (10001), (10001), (1000 v), (1000 v), (0101 v)¹², (010 ω 1), (010 ω 1),
(0010 v), (0010 v), (00011), (00011), (0001 ω), (0001 v), (0001 v), (0001 v), (001 ω 1), (001 ω 1),
(010 v 1), (0101 ω), (010 ω 1), (010 v 1), (100 ω 0), (100 v 0), (10010), (100 ω 0), (100 v 0), (100 v 0),
(001 ω 1), (001 v 1), (001 ω 1), (001 v 1), (001 ω 1), (001 v 1), (001 ω 1), (001 v 1), (001 ω 1), (001 v 1),
(11000)¹, (11000)³, (11000), (11000), (11010)⁶, (11011), (110 ω 0), (110 ω 1), (110 ω 1), (110 ω 1),
(00001), (00111), (0011 ω), (0011 v), (00111), (00111), (0011 ω), (0011 v), (0011 v), (0011 v),
(1100 v)⁶, (1100 ω), (11001), (11001), (11001), (11001), (11001), (11001), (11001), (11001),
(10001), (1000 v), (1000 ω), (10011)⁶, (100 ω 1), (100 ω 1), (100 ω 1), (10001), (10001), (10001),
(01101), (01 ω 0 v), (01 v 0 ω), (01001), (0100 v), (0100 ω), (01101), (01 ω 0 v), (01 v 0 ω), (01010),
(10 ω 00), (10 v 00), (10100)³, (10 ω 00), (10 ω 00), (10 v 00), (10100)³, (10 ω 00), (10 ω 00), (10101), (10101),
(10 ω 00), (10 v 00), (10101), (10 ω 00), (10 ω 00), (10 v 00), (10101), (10 ω 00), (10 ω 00), (10101),
(10 ω 1 v), (10 v 1 v), (10 v 1 v), (10 v 1 v), (10 v 1 v), (10 v 1 v), (10101), (10 v 1 v), (10 v 1 v), (10 v 1 v),
(010 ω 1), (010 ω 1), (010 ω 1), (010 v 1), (010 v 1), (010 v 1), (01011), (01 ω 1 ω), (01 ω 1 ω), (01 ω 1 ω),
(101 ω)¹², (101 v 1), (101 v 1), (10 ω 11), (10 ω 11), (10 ω 11), (10 ω 11), (10 ω 11), (10 ω 11), (10 ω 11),
(0101 ω), (0101 ω), (010 ω 1), (010 ω 1), (010 v 1), (010 v 1), (010 v 1), (010 v 1), (010 v 1), (010 v 1),
(1010 v), (1010 ω), (1010 ω)⁶, (1010 ω), (1010 ω), (1010 ω), (1010 ω), (1010 ω), (1010 ω), (1010 ω),
(01 v 1 ω), (01 v 1 ω), (01 v 1 ω), (01 v 1 ω), (01 v 1 ω), (01 v 1 ω), (01 v 1 ω), (01 v 1 ω), (01 v 1 ω), (01 v 1 ω),
(10 ω 1), (10 ω 1), (10 ω 1), (10 v 1), (10 v 1), (10 v 1), (10 v 1), (10 v 1), (10 v 1), (10 v 1),
(0101 v), (010 v 1), (0101 ω), (010 ω 1), (010 ω 1), (0111 v), (0111 v), (01 ω 1 ω), (01 ω 1 ω), (01 ω 1 ω),

$(101\omega v)^{12}, (101v\omega), (10\omega 11), (10\omega v\omega), (10v11), (10v\omega v), (10100), (10100), (10\omega 00), (10\omega 00),$
 $(010\omega 0), (010v0), (01010), (010v0), (01010), (010\omega 0), (011\omega 1), (011v1), (01\omega 1v), (01\omega vv),$
 $(10v00), (10v00), (101v1)^{12}, (101\omega 1), (10\omega vv), (10\omega 1v), (10v\omega\omega), (10v1\omega), (10\omega 0v), (10v0\omega),$
 $(01v1\omega), (01v\omega\omega), (010\omega v), (010v\omega), (01011), (010v\omega), (01011), (010\omega v), (011v\omega), (011\omega v),$
 $(10101), (10v0\omega), (10101), (10\omega 0v), (10011)^6, (10010), (100\omega v), (100\omega 0), (100v\omega), (100v0),$
 $(01\omega vv\omega), (01\omega 11), (01v\omega v), (01v11), (01100), (01101), (01\omega 00), (01\omega 0v), (01v00), (01v0\omega),$
 $(1001v)^6, (1001\omega), (100\omega\omega), (100\omega 1), (100vv), (100v1), (100\omega v)^{12}, (100\omega v), (100vv), (100v\omega),$
 $(0110\omega), (0110v), (01\omega 01), (01\omega 0\omega), (01v01), (01v0v), (01101), (0110\omega), (01101), (0110v),$
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 $(01\omega 0\omega), (01\omega 0v), (01\omega 01), (01\omega 0v), (01v0\omega), (01v0v), (01v01), (01v0\omega), (011\omega 0), (011v0),$
 $(101\omega 0), (101v0), (1001v), (100vv), (10\omega 10), (10\omega v0), (1001\omega), (100\omega\omega), (10v10), (10v\omega 0),$
 $(0110\omega), (0110v), (01\omega 10), (01\omega v0), (01\omega 01), (01\omega 0\omega), (01v10), (01v\omega 0), (01v01), (01v0v),$
 $(10111)^6, (10110), (10\omega\omega v), (10\omega\omega 0), (10vv\omega), (10vv0), (101\omega v)^{12}, (101v\omega), (10\omega\omega 0), (10vv0),$
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 $(10110), (10\omega 11), (10\omega vv), (10vv0), (10110), (10\omega\omega 0), (10v11), (10vv\omega), (101\omega v)^{12}, (101v\omega),$
 $(01\omega 1v), (01\omega\omega 0), (01\omega\omega 0), (01vvv), (01v1\omega), (01v\omega\omega), (01vv0), (01vv0), (0111v), (0111\omega),$
 $(10\omega\omega 1), (10vv1), (1011v), (10\omega 11), (10\omega vv), (10vvv), (1011\omega), (10\omega\omega\omega), (10v11), (10vv\omega),$
 $(011\omega 1), (011v1), (01\omega 1v), (01\omega\omega 1), (01\omega\omega\omega), (01\omega vv), (01v1\omega), (01v\omega\omega), (01vv1), (01vvv),$
 $(1011\omega)^{12}, (1011v), (10\omega 11), (10v11), (101\omega v), (10\omega\omega\omega), (10\omega\omega 1), (10vv\omega), (101v\omega), (10\omega vv),$
 $(011\omega 1), (011v1), (0111\omega), (0111v), (01\omega\omega\omega), (01\omega 1v), (01\omega vv), (01\omega\omega 1), (01vvv), (01vv1),$
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 $(01v1\omega), (01v\omega\omega), (011\omega\omega), (011vv), (01110), (01110), (01\omega\omega 0), (01\omega 1\omega), (01\omega v1), (01\omega\omega 0),$
 $(101vv), (10\omega v1), (10vv0), (10vv0), (10111)^{12}, (10111), (10\omega 1\omega), (10v1v), (101\omega\omega), (10\omega\omega v),$
 $(01vv0), (01vv0), (01v1v), (01v\omega 1), (011\omega\omega), (011vv), (01111), (01111), (01\omega\omega v), (01\omega 1\omega),$
 $(10\omega\omega v), (10\omega v1), (101vv), (10\omega v1), (10vvv), (10vvv), (101v1)^{12}, (101\omega 1), (10\omega v1), (10vv1),$
 $(01\omega v1), (01\omega\omega v), (01vv\omega), (01vv\omega), (01v1v), (01v\omega 1), (011\omega\omega), (011vv), (011v\omega), (011\omega v),$
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 $(01\omega vv\omega), (01\omega 1\omega), (01\omega v1), (01\omega 11), (01v\omega v), (01v11), (01v1v), (01v\omega 1), (0111\omega), (0111v),$
 $(1011\omega), (10vv1), (1011v), (10\omega\omega 1), (10\omega v0)^{12}, (10\omega\omega v), (10vv0), (10vv\omega), (101v0), (10111),$
 $(01\omega\omega\omega), (01\omega\omega 1), (01vvv), (01vv1), (01111), (011v0), (01111), (011\omega 0), (01\omega\omega v), (01\omega v0),$
 $(10vv\omega), (10v10), (10111), (101\omega 0), (10\omega\omega v), (10\omega 10), (10\omega 1v)^{12}, (10\omega 10), (10v1\omega), (10v10),$
 $(01\omega 10), (01\omega\omega v), (01v\omega 0), (01vv\omega), (01v10), (01vv\omega), (011\omega 0), (011v0), (011\omega 0), (011v0),$
 $(101\omega 10), (10v10), (101\omega 0), (10\omega 10), (10\omega 1\omega)^{12}, (10\omega 10), (10v1v), (10v10), (101\omega\omega), (101\omega 0),$
 $(01\omega 10), (01\omega v0), (01v10), (01v\omega 0), (011v0), (011vv), (011\omega 0), (011\omega\omega), (01\omega v0), (01\omega v1),$
 $(10v\omega 1), (10v\omega 0), (101vv), (101v0), (10\omega v1), (10\omega vv), (10\omega 1\omega)^6, (10v1v), (101\omega\omega), (10v\omega 1),$
 $(01\omega 10), (01\omega 1\omega), (01v\omega 0), (01v\omega 1), (01v10), (01v1v), (011vv), (011\omega\omega), (01\omega v1), (01\omega 1\omega),$
 $(101vv), (10\omega v1),$